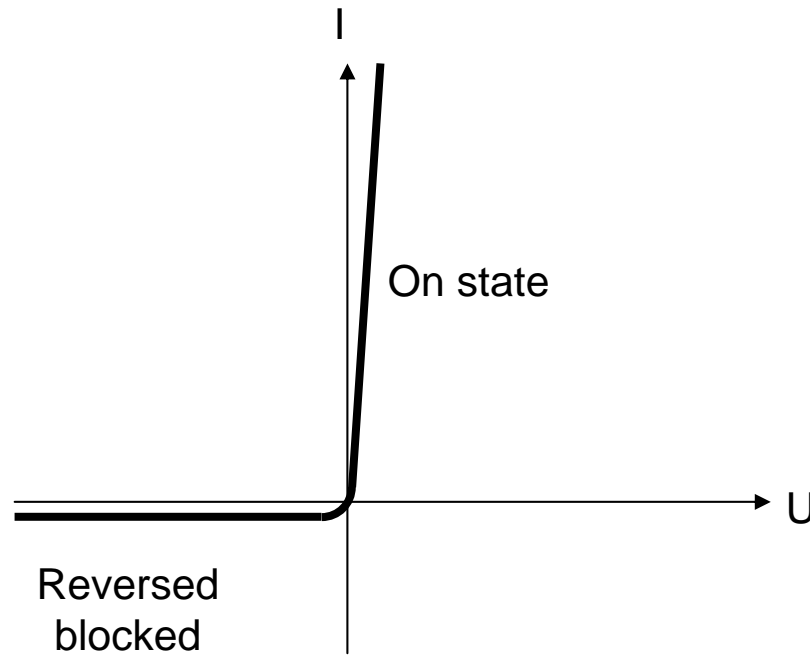
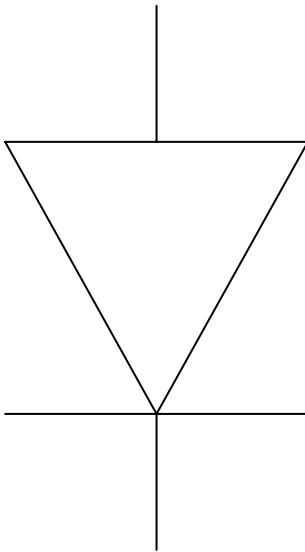


Diode and Thyristor based converters

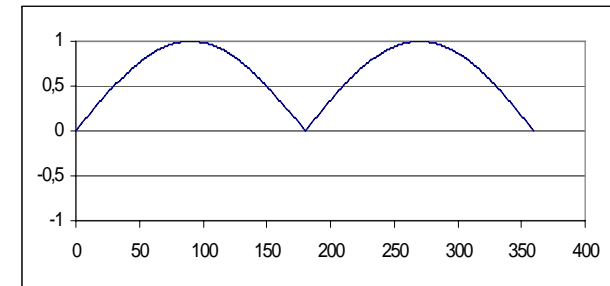
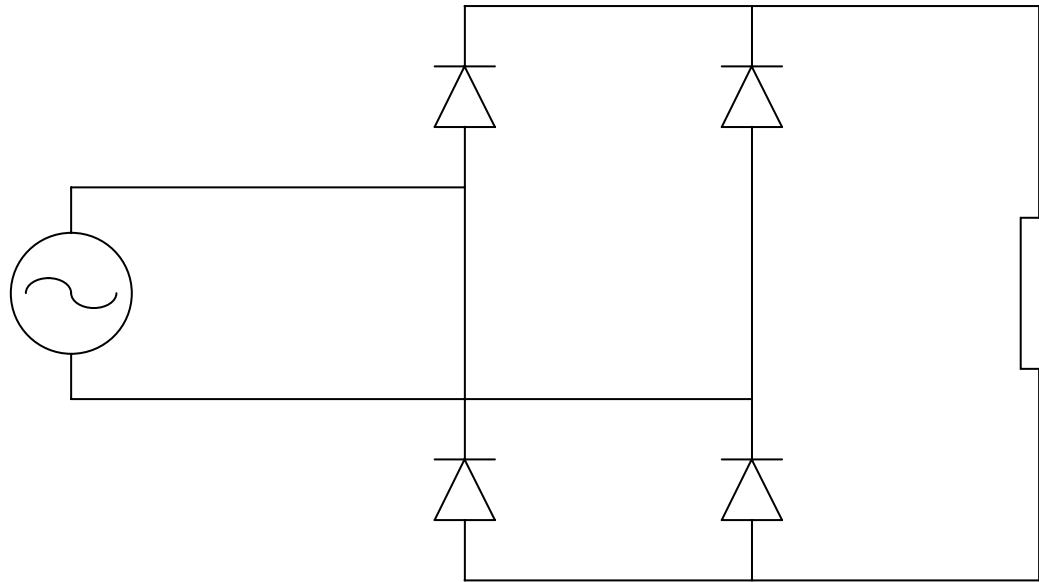
= *Line (or load) commutated converters*



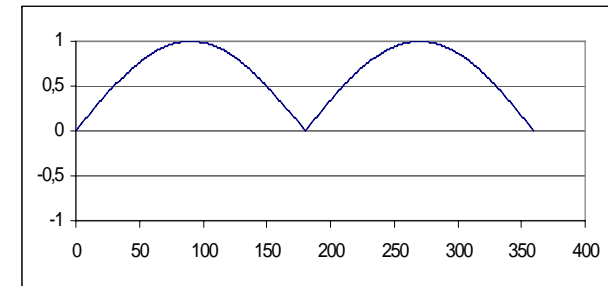
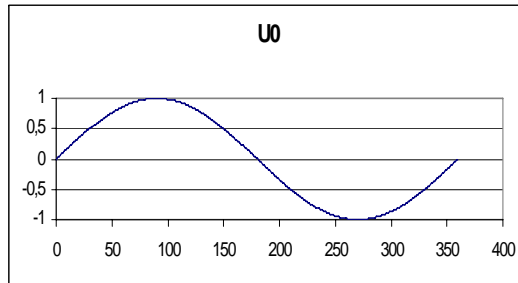
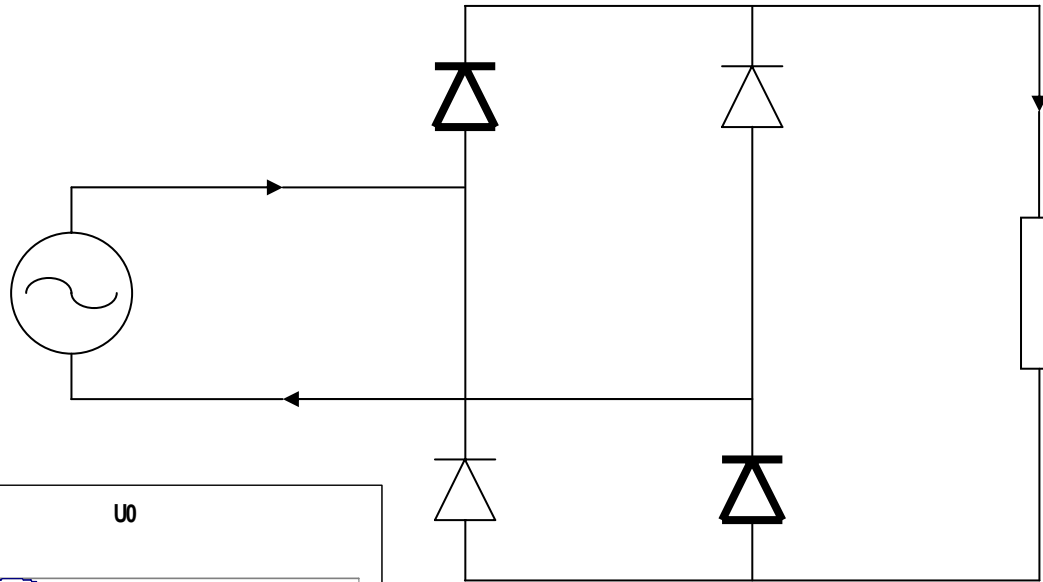
Diode



Single phase diode rectifier ideal

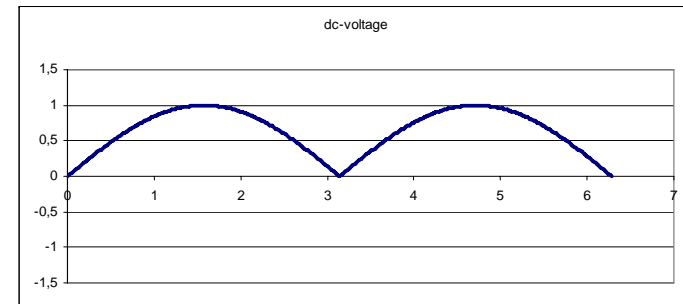
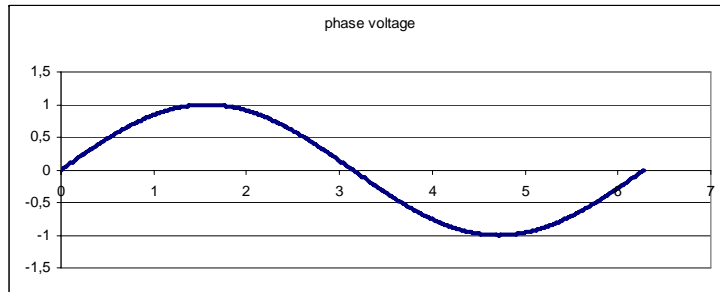
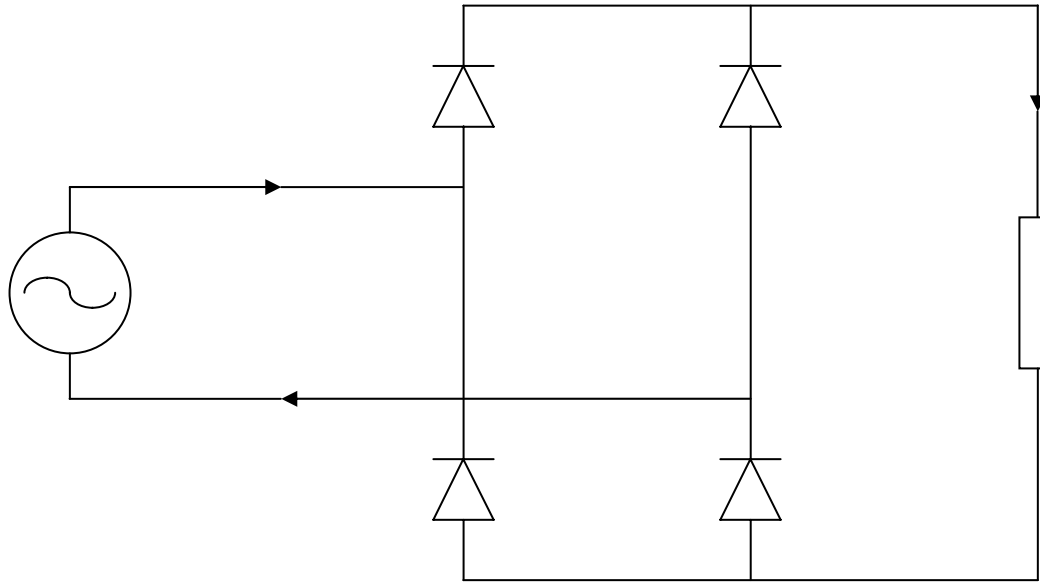


Single phase diode rectifier ideal



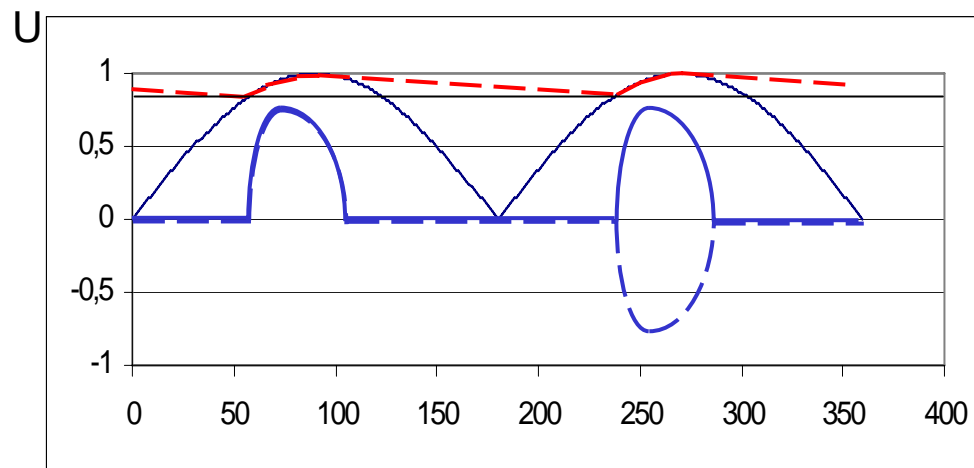
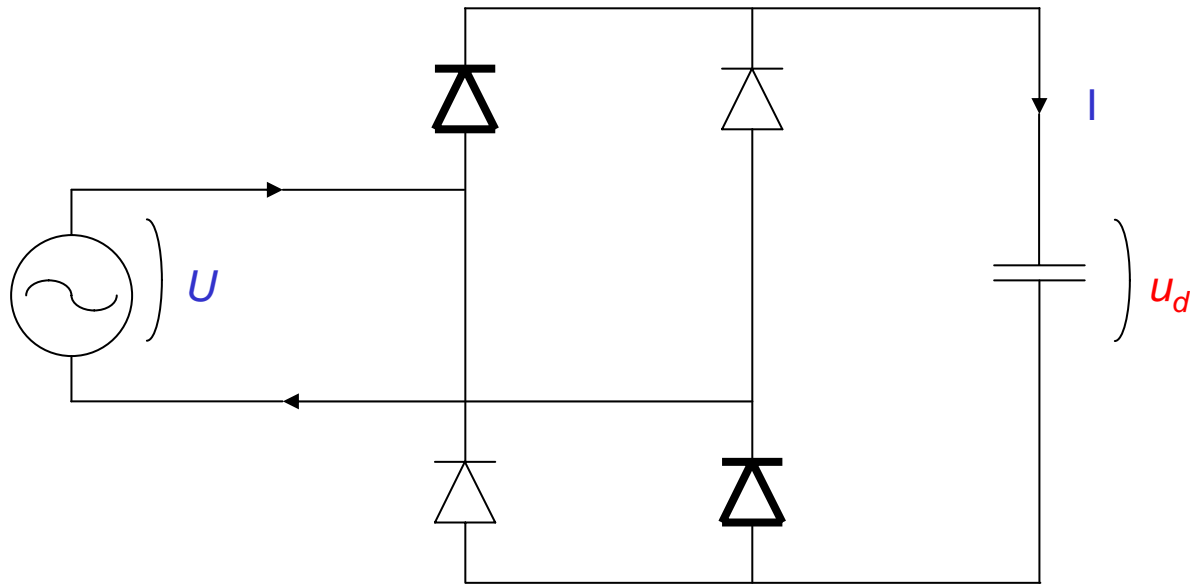
Single phase diode rectifier

AC-side and DC side voltage

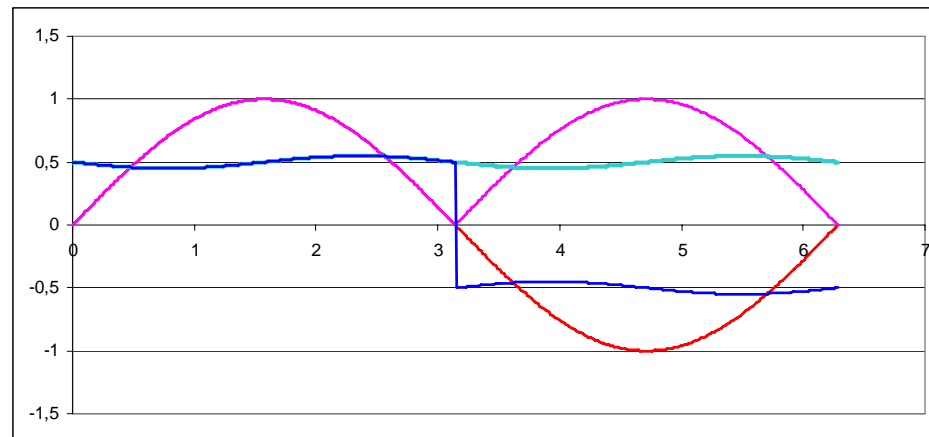
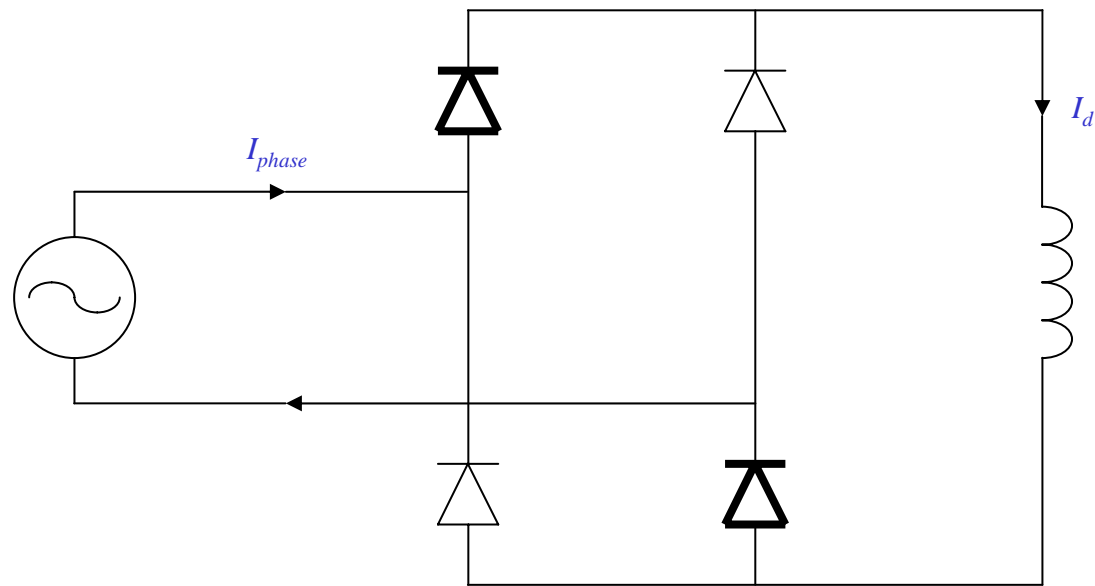


$$V_{dc} = \frac{1}{T/2} \int_{T/2}^{\pi/2} \hat{e}_{LN} \sin(\omega t) dt = \frac{\hat{e}_{LN}}{\pi} \int_{-\pi/2}^{\pi/2} \sin(\omega t) d(\omega t) = \frac{2}{\pi} \hat{e}_{LN} = \frac{2\sqrt{2}}{\pi} E_{LN}$$

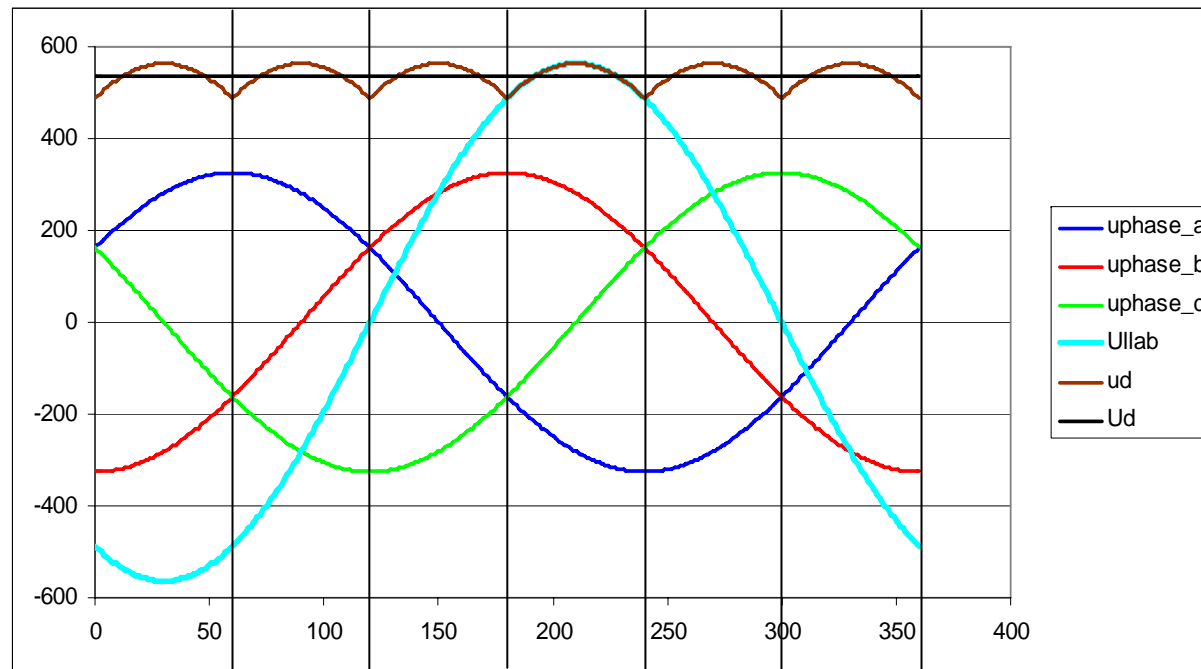
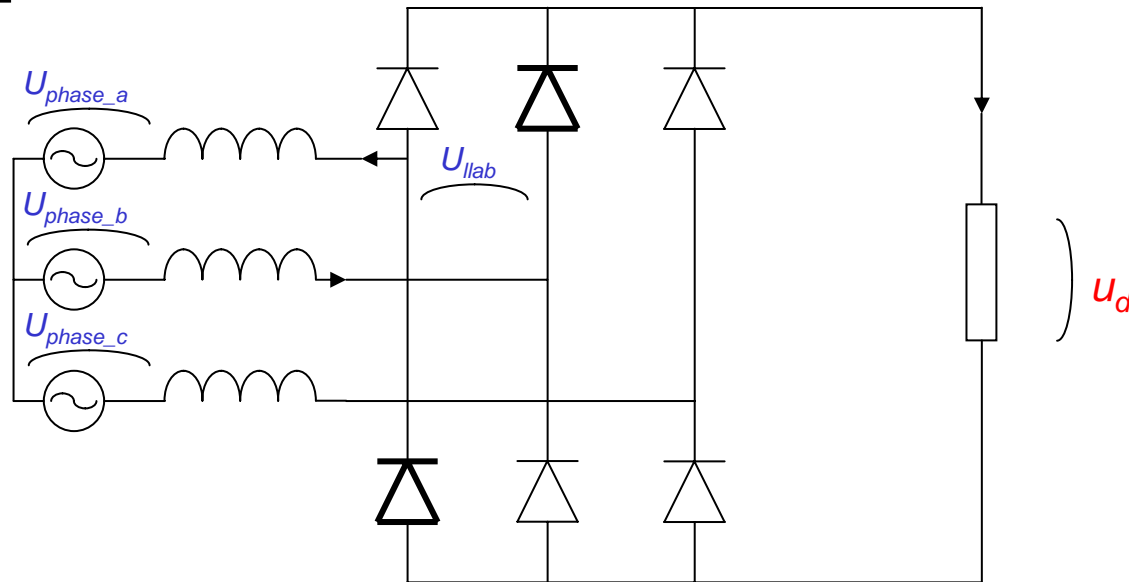
Single phase diode rectifier with capacitive load



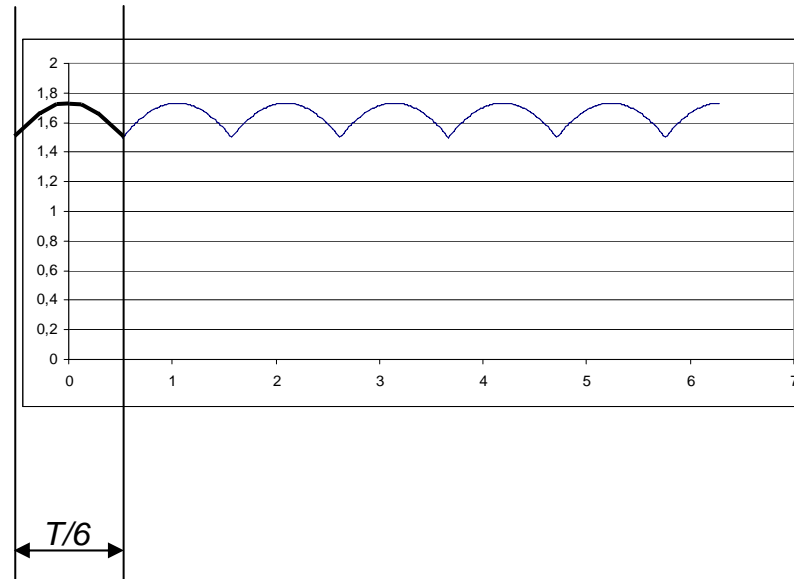
Single phase diode rectifier with inductive load



Three phase diode rectifier with resistive load

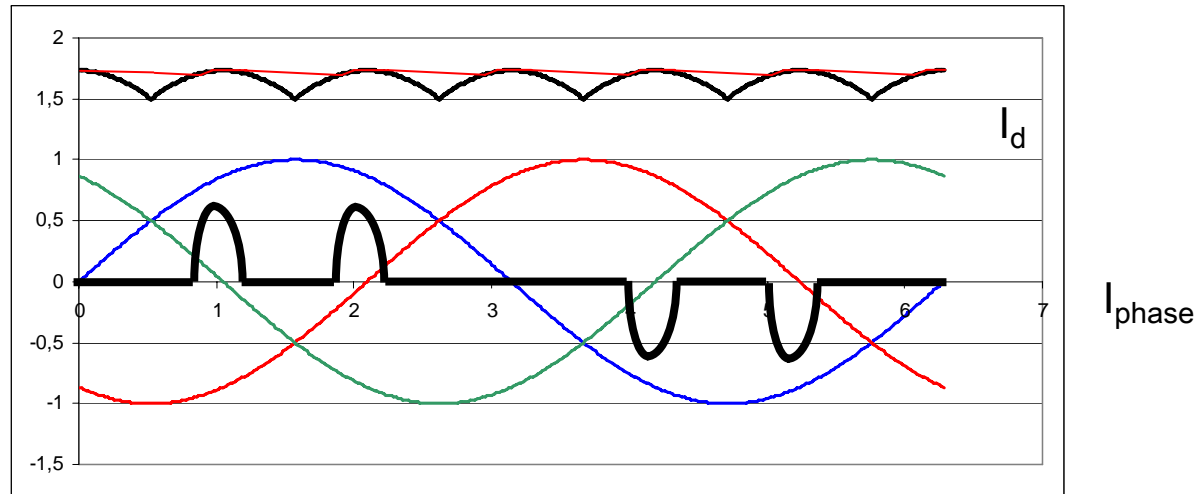
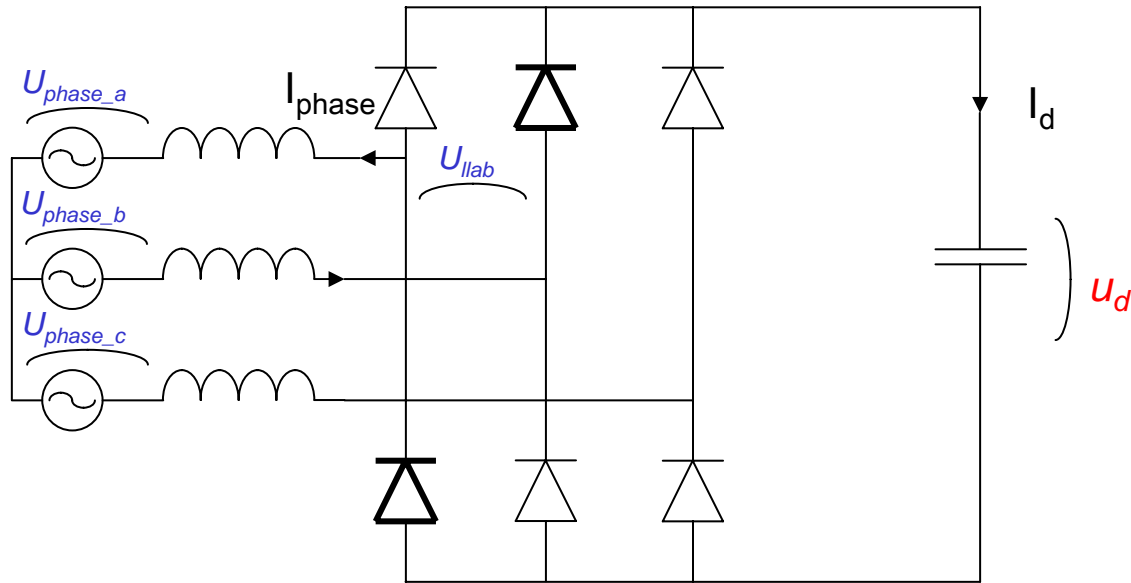


Three phase diode rectifier voltage

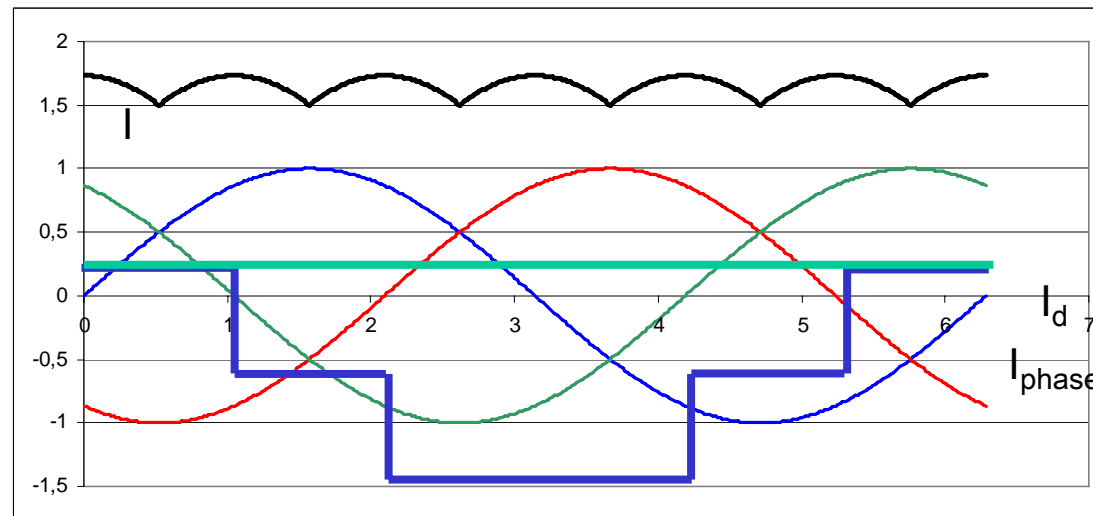
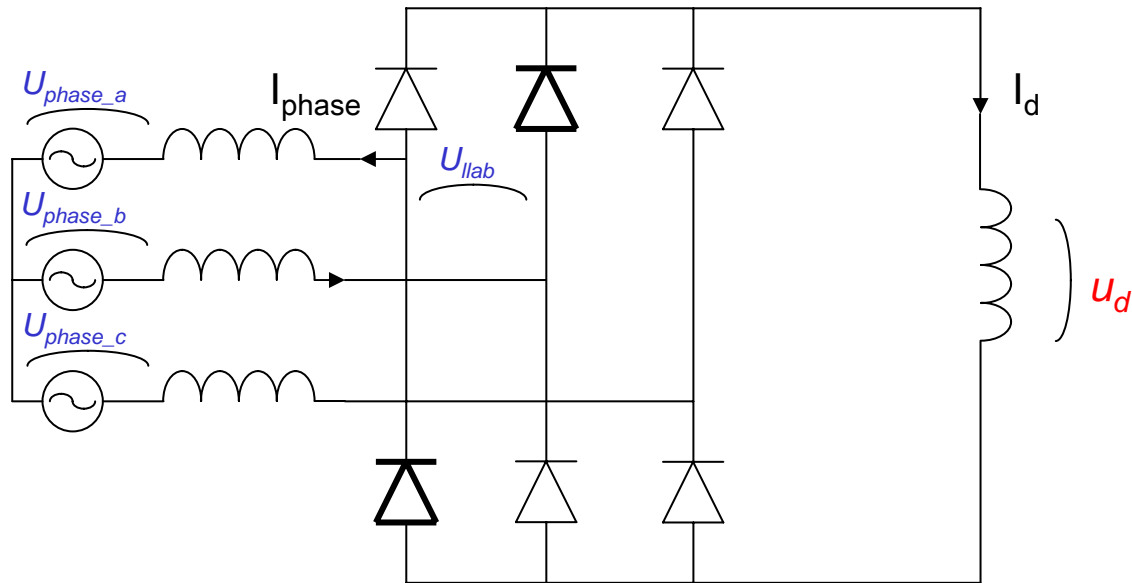


$$V_{dc} = \frac{\hat{e}_{LL}}{T/6} \int_{T/6} \cos(\omega t) dt = \frac{\hat{e}_{LL}}{\pi/3} \int_{-\pi/6}^{\pi/6} \cos(\omega t) d(\omega t) = \frac{3 \cdot \hat{e}_{LL}}{\pi} = \frac{3\sqrt{2} \cdot E_{LL\text{eff}}}{\pi} = \frac{3\sqrt{3} \cdot \hat{e}_{LN}}{\pi}$$

Three phase diode rectifier with capacitive load

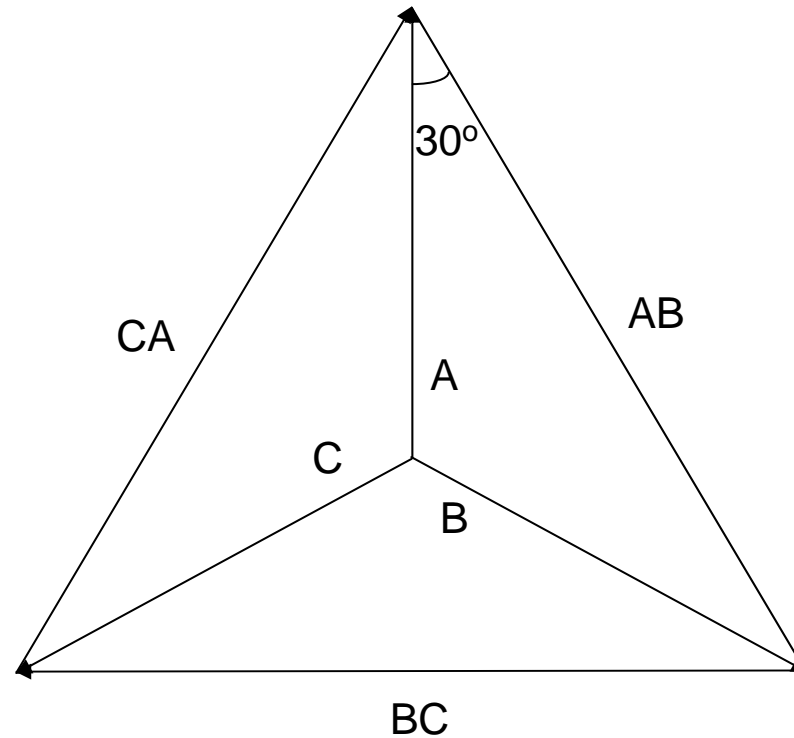


Three phase diode rectifier with inductive load

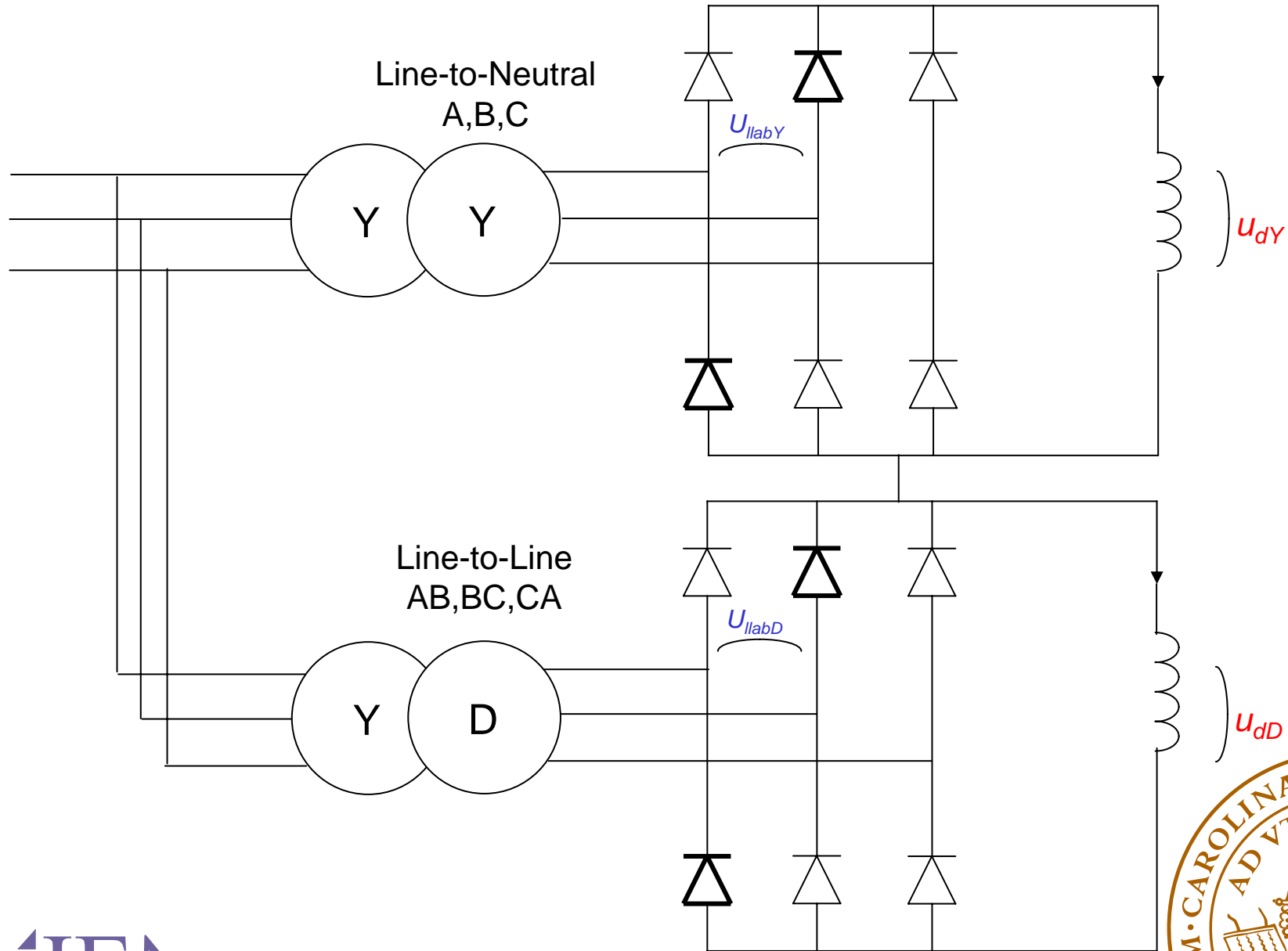


Three phase voltage phasors

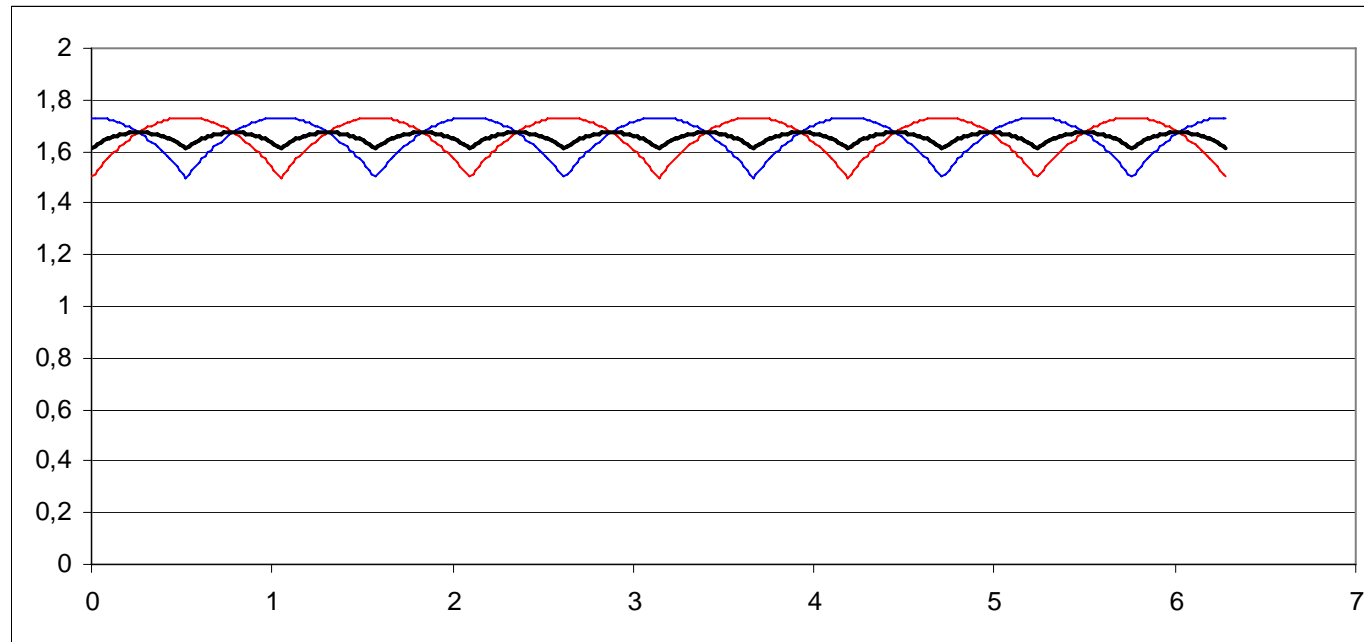
Line-to-Neutral and Line-to-Line



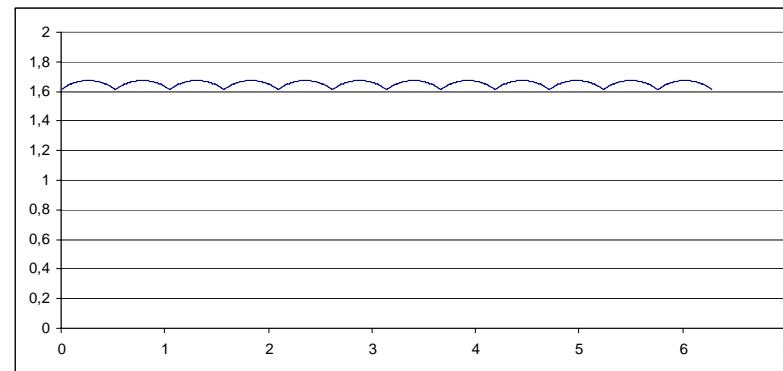
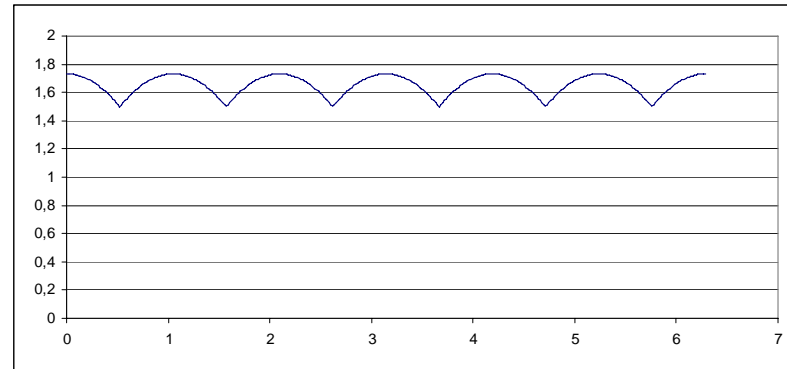
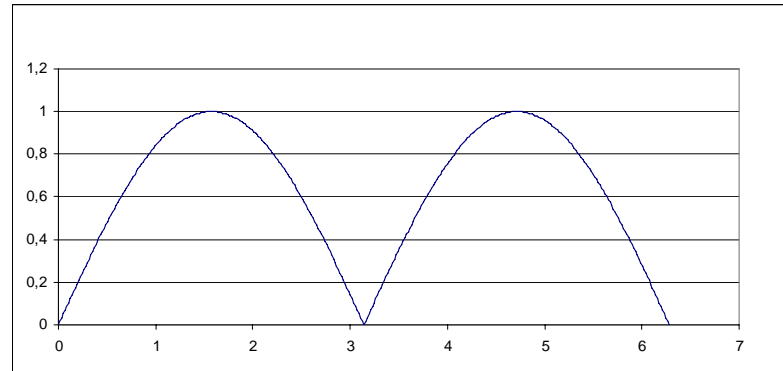
“Twelve pulse” rectifier



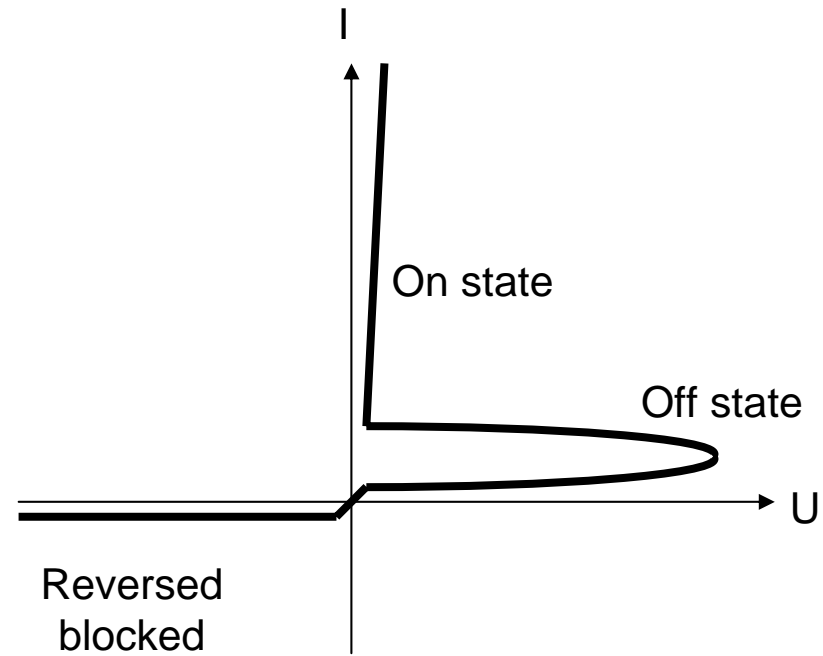
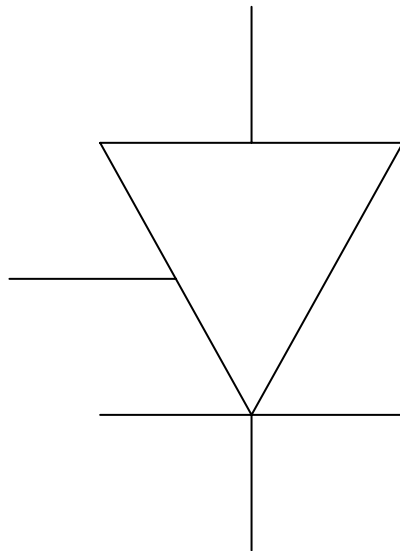
“Twelve pulse” rectifier



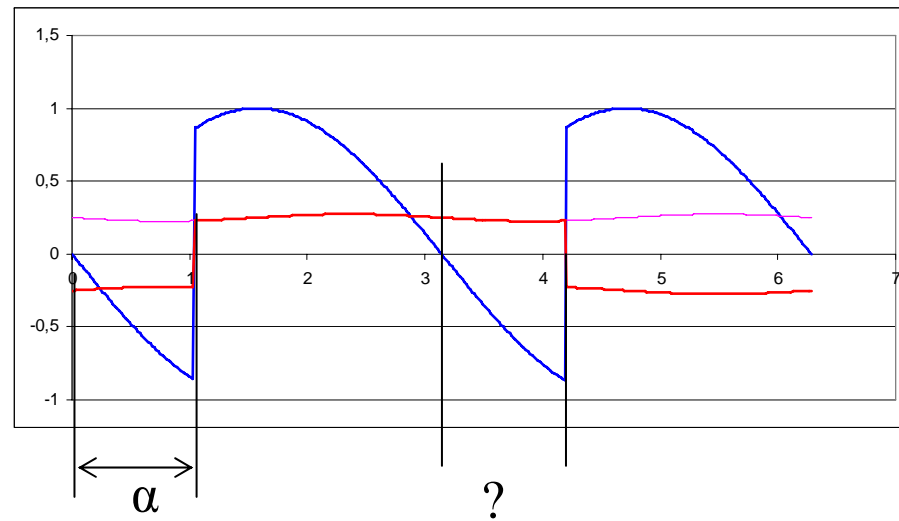
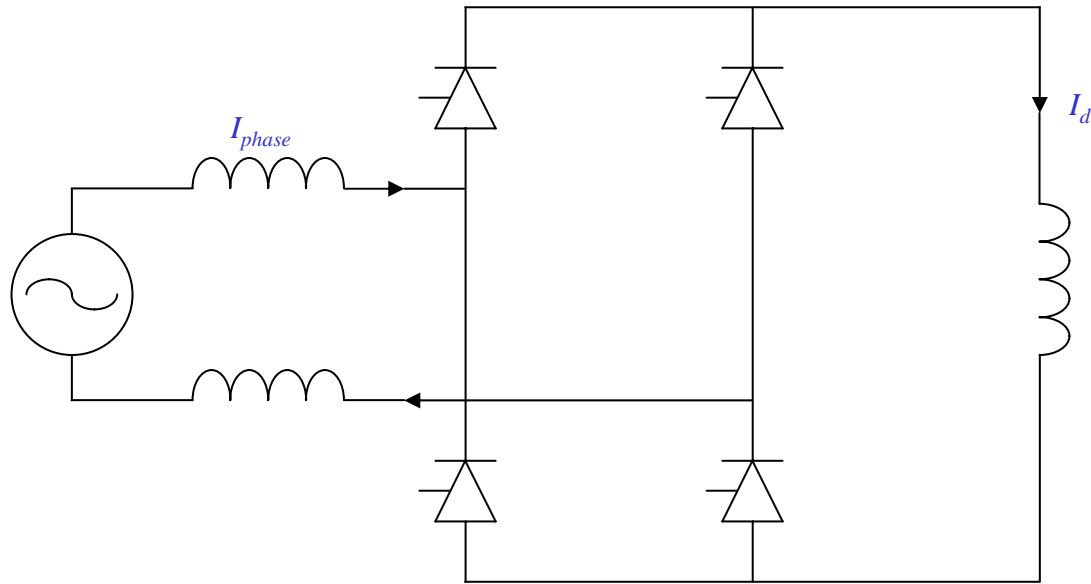
Ripple reduction



Thyristor



Single phase thyristor rectifier with inductive load

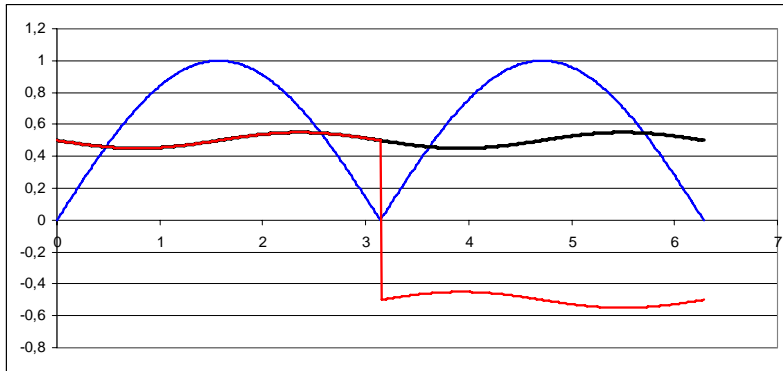


Single phase thyristor rectifier voltage

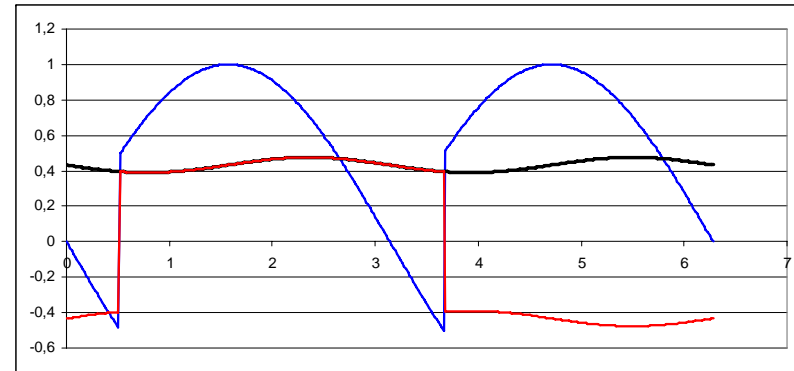
$$V_{dc} = \cos(\alpha) \cdot \frac{1}{T/2} \int_{T/2} \hat{e}_{LN} \sin(\omega t) dt = \cos(\alpha) \cdot \frac{\hat{e}_{LN}}{\pi} \int_{-\pi/2}^{\pi/2} \sin(\omega t) d(\omega t) = \cos(\alpha) \cdot \frac{2}{\pi} \hat{e}_{LN} = \cos(\alpha) \cdot \frac{2\sqrt{2}}{\pi} E_{LN} = V_{dc0} \cdot \cos(\alpha)$$

Single phase thyristor rectifier with inductive load

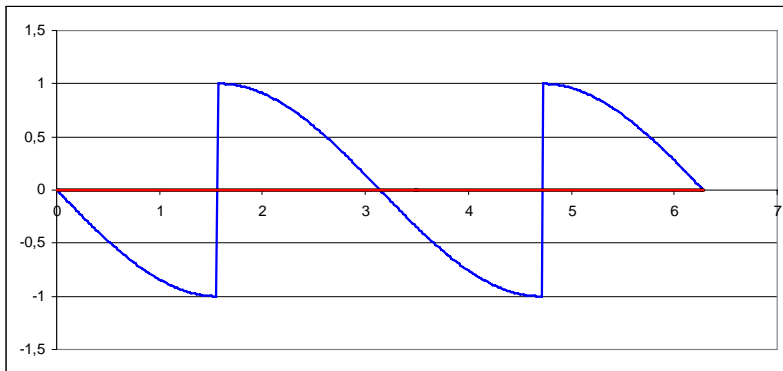
Different ignition angles



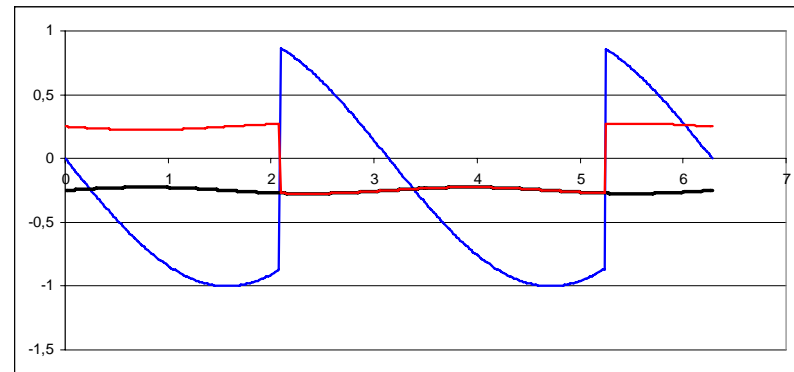
$\alpha = 0^\circ$



$\alpha = 30^\circ$

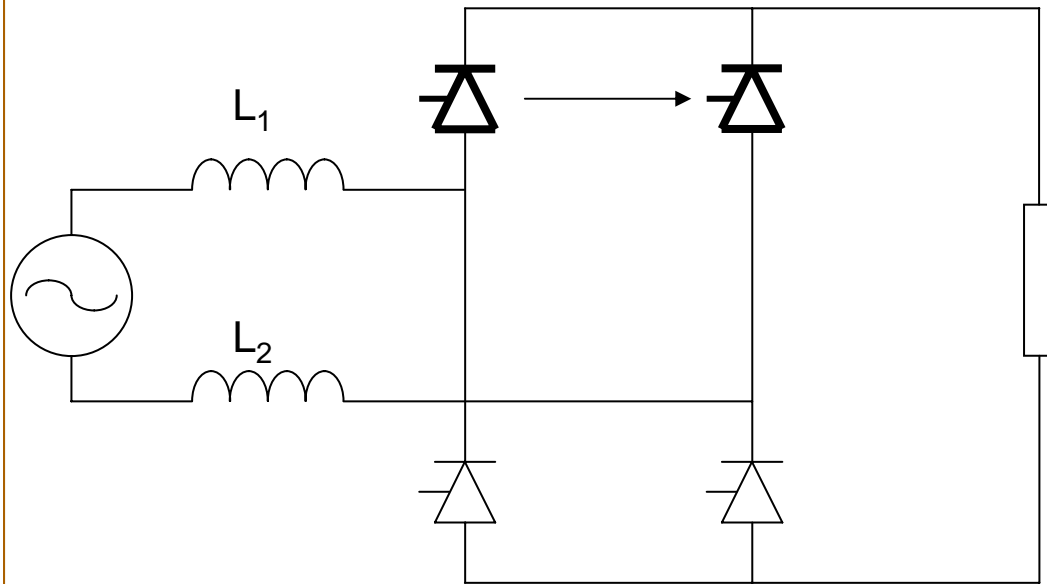


$\alpha = 90^\circ$



$\alpha = 120^\circ$

Commutation time in single phase thyristor rectifier with phase inductance

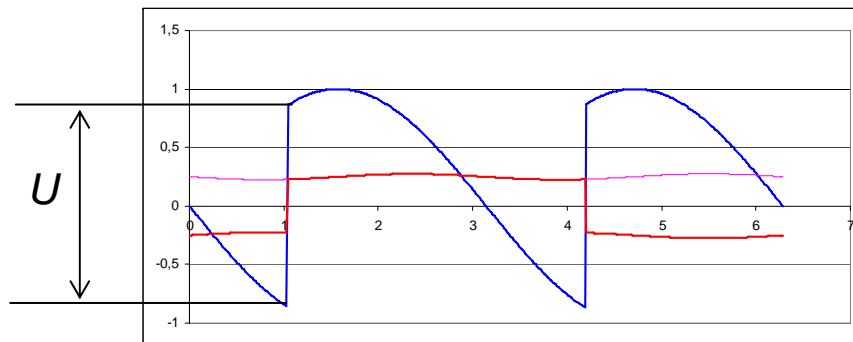


$$L = L_1 + L_2$$

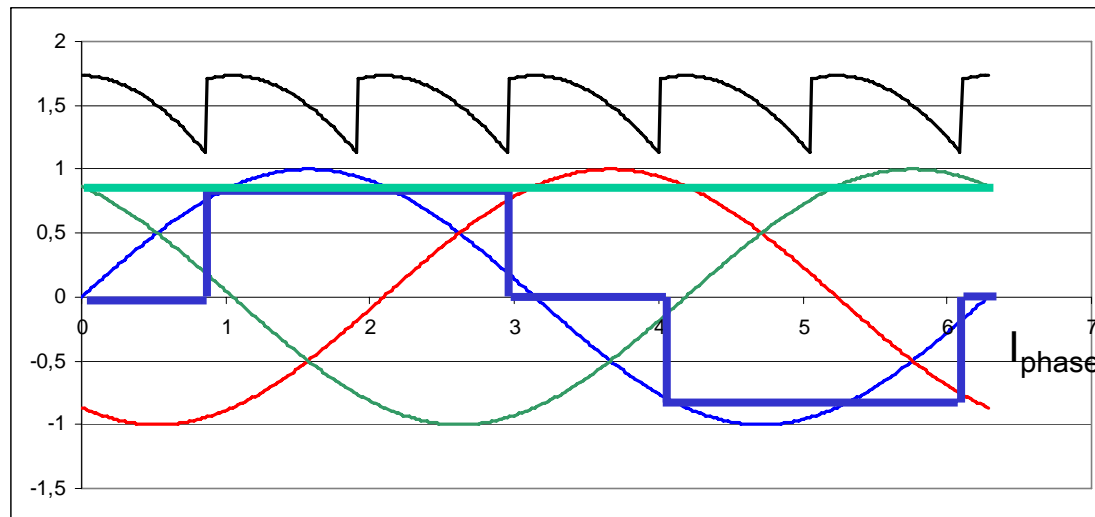
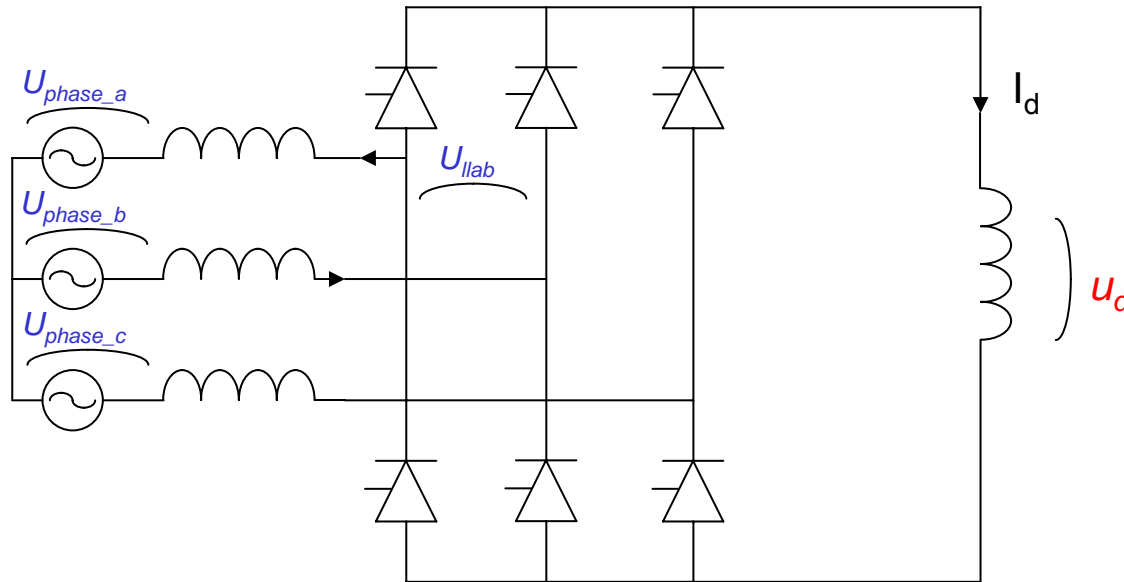
$$U = L \cdot \frac{di}{dt} \approx L \cdot \frac{\Delta i}{\Delta t}$$

$$\Delta t = \frac{L \cdot \Delta i}{U}$$

The time can be very long with low voltage and high inductance



Three phase thyristor rectifier with inductive load

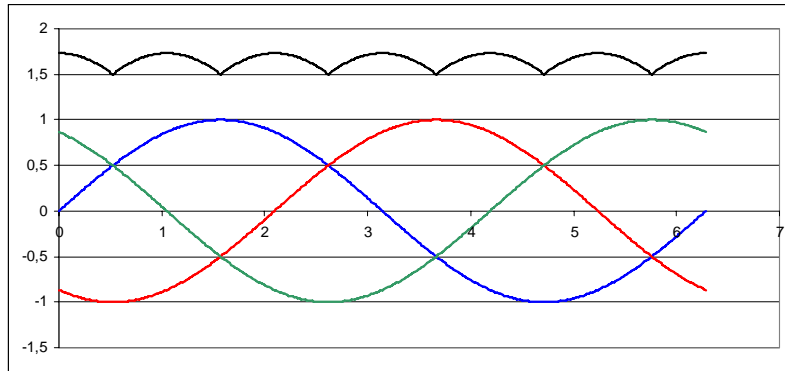


Three phase thyristor rectifier output voltage

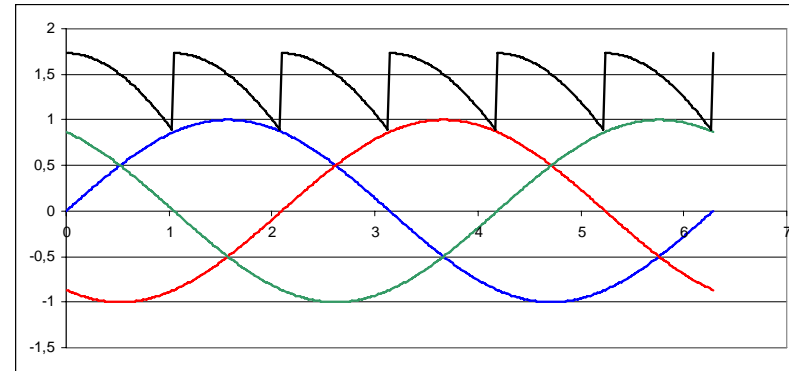
$$V_{dc} = \cos(\alpha) \cdot \frac{\hat{e}_{LL}}{T/6} \int_{T/6} \cos(\omega t) dt = \cos(\alpha) \cdot \frac{\hat{e}_{LL}}{\pi/3} \int_{-\pi/6}^{\pi/6} \cos(\omega t) d(\omega t) = \cos(\alpha) \cdot \frac{3 \cdot \hat{e}_{LL}}{\pi} = \cos(\alpha) \cdot \frac{3\sqrt{2} \cdot E_{LL\text{eff}}}{\pi} = \cos(\alpha) \cdot \frac{3\sqrt{3} \cdot \hat{e}_{LN}}{\pi} = V_{dc0} \cdot \cos(\alpha)$$

Three phase thyristor rectifier with inductive load

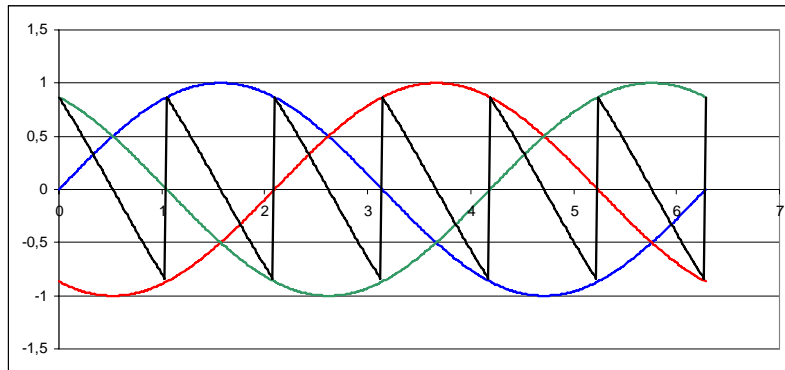
Different ignition angles



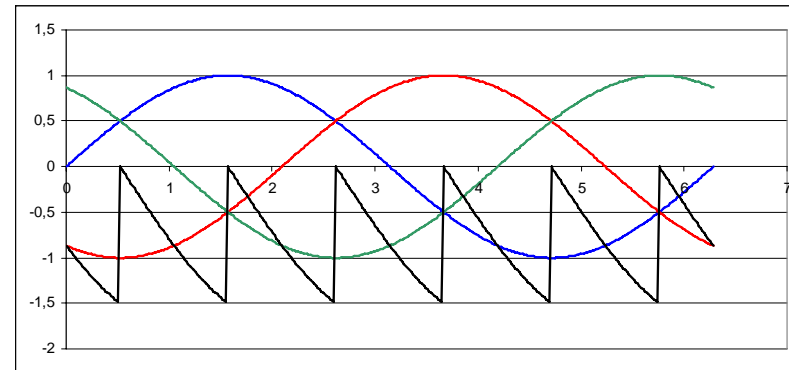
$\alpha=0^\circ$



$\alpha=30^\circ$

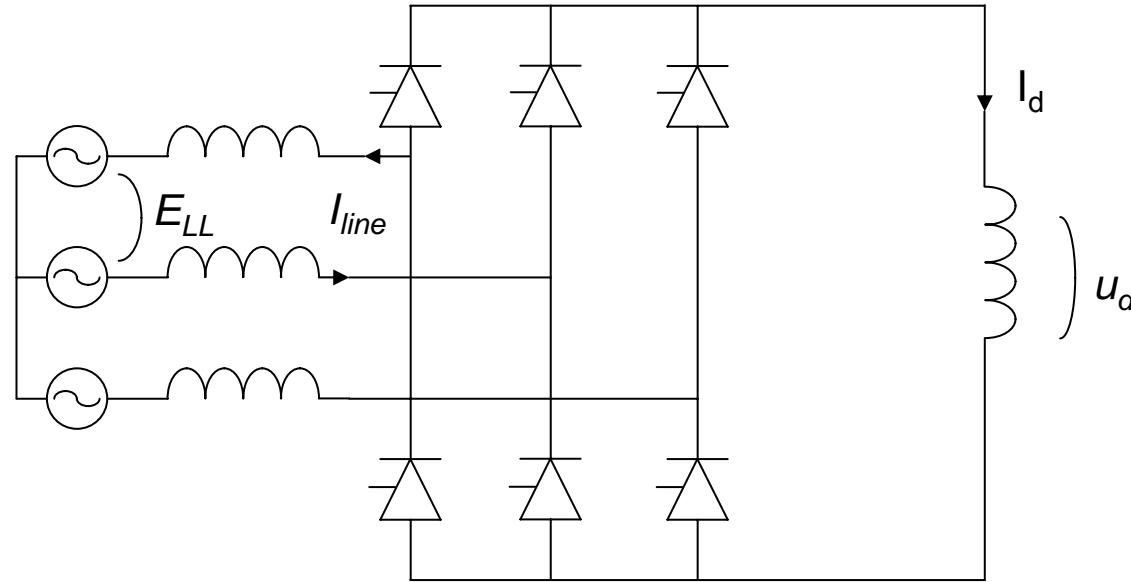


$\alpha=90^\circ$



$\alpha=120^\circ$

Three phase thyristor rectifier with inductive load



Active power

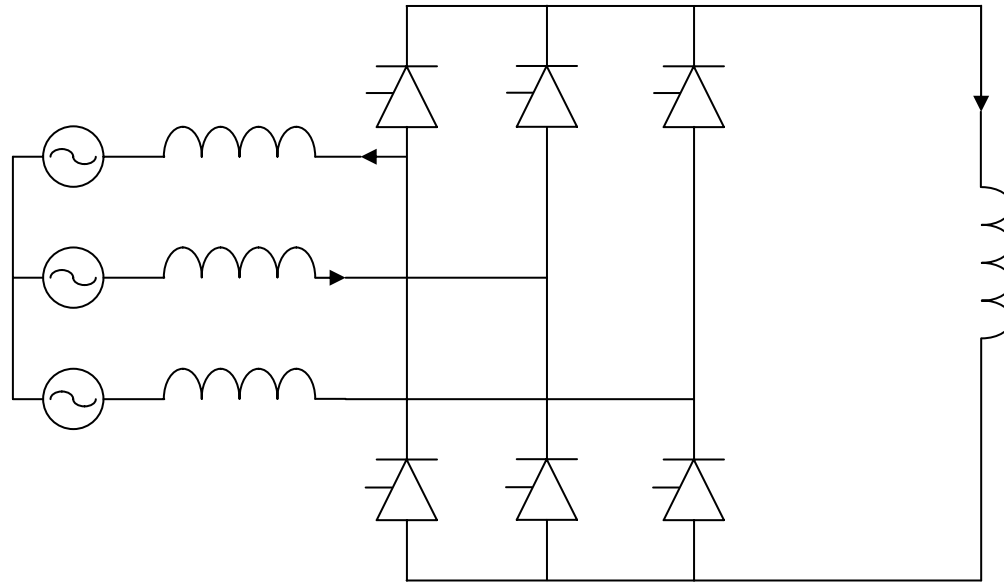
$$P = \sqrt{3} \cdot E_{LL} \cdot I_{Line} \cdot \cos(\alpha)$$

Reactive power

$$Q = \sqrt{3} \cdot E_{LL} \cdot I_{Line} \cdot \sin(\alpha)$$

Three phase thyristor converter

Power direction



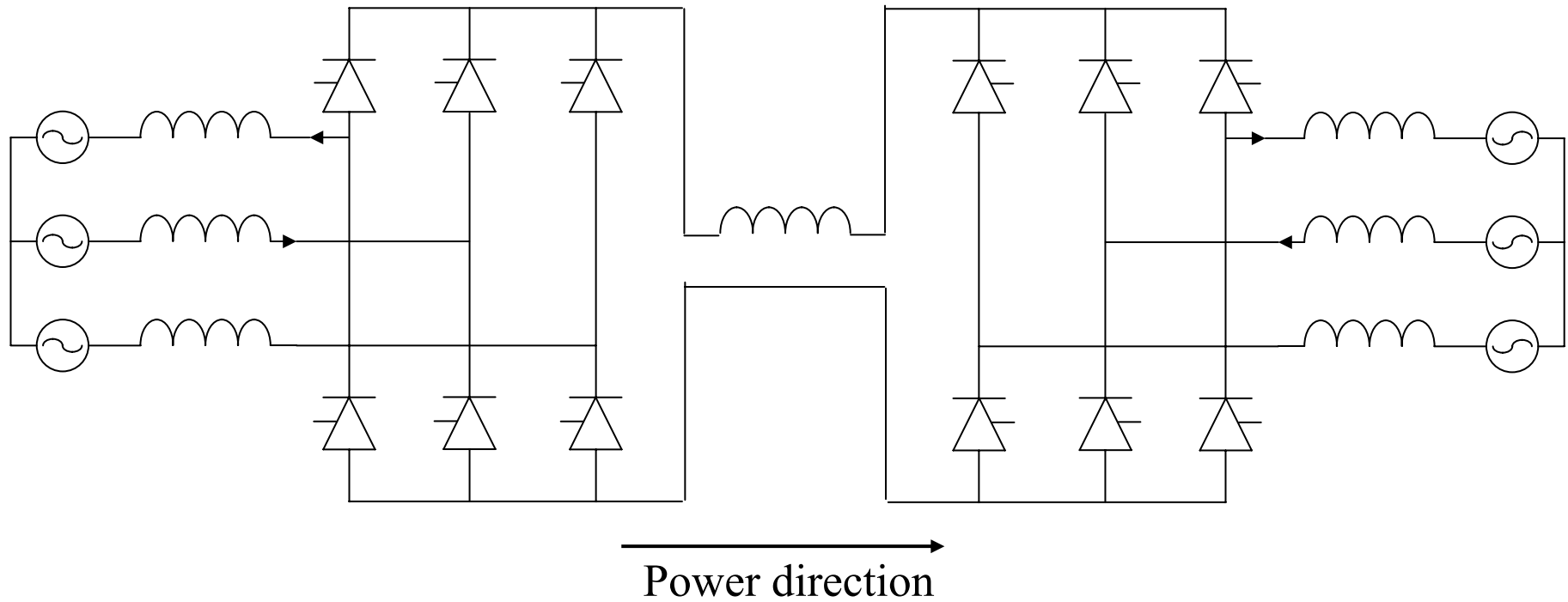
$0^\circ < \alpha < 90^\circ$

Power direction from AC-side to DC-side

$90^\circ < \alpha < 180^\circ$

Power direction from DC-side to AC-side

HVDC



$$0^\circ < \alpha < 90^\circ$$

$$90^\circ < \alpha < 180^\circ$$

HVDC

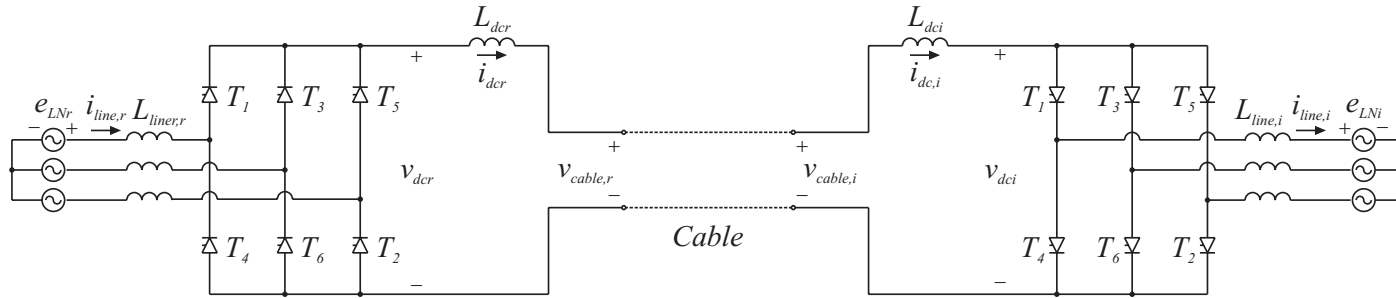


Figure 1.10: Principal schematic of a HVDC power transmission system.

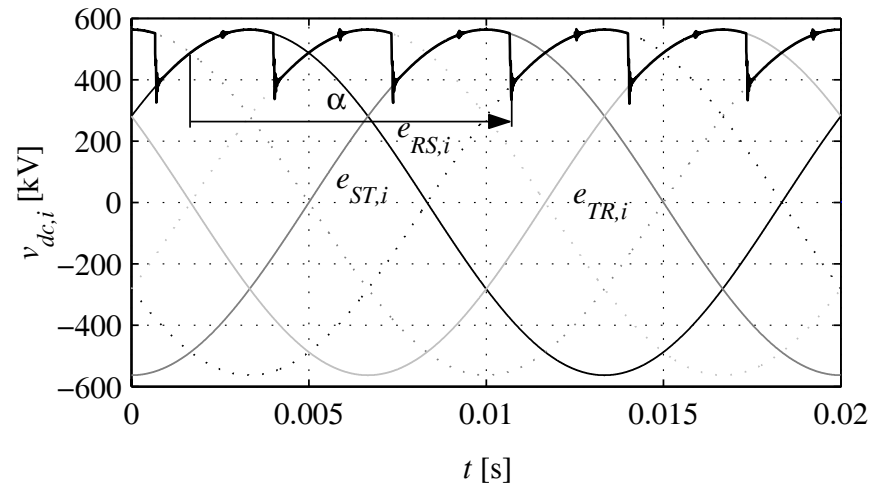
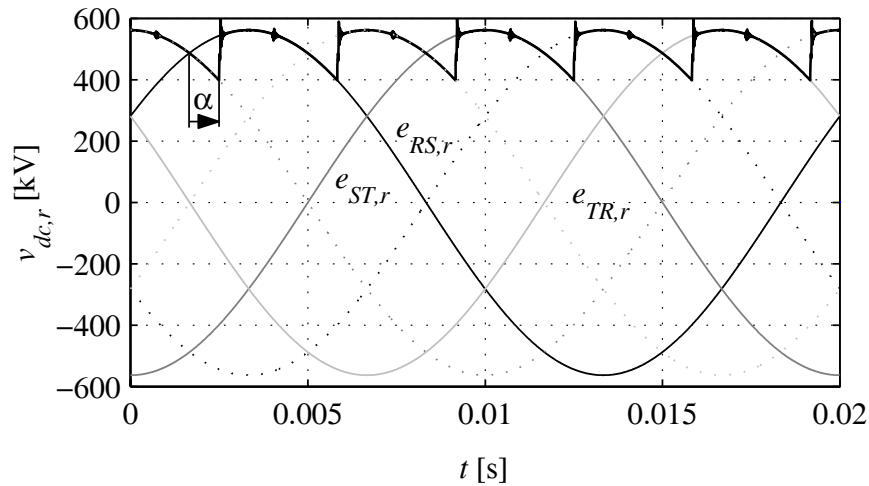


Figure 1.11: Line-to-line voltages, DC side voltage and control angles for the rectifier (left) and inverter (right) of an HVDC transmission system.

HVDC Converter Currents

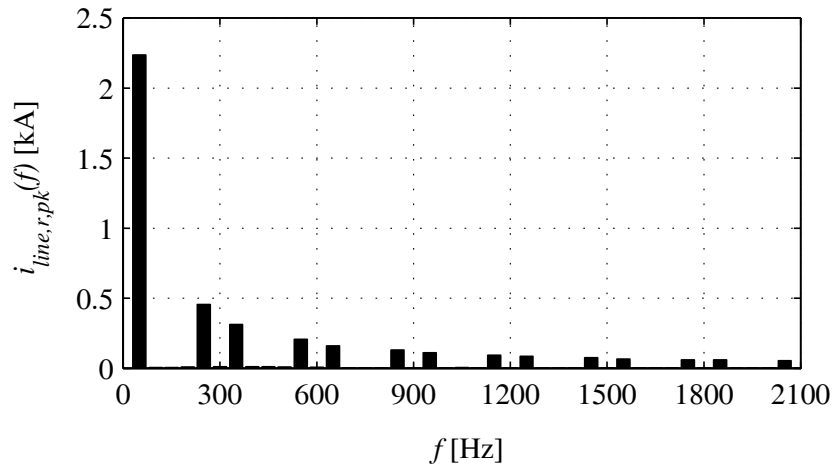
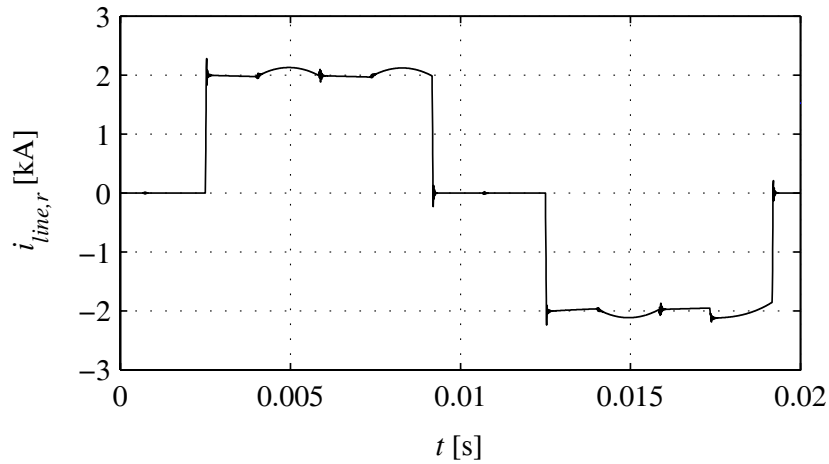


Figure 1.12: R-phase line current (top) and its spectrum (bottom) for the rectifier of an HVDC transmission system.

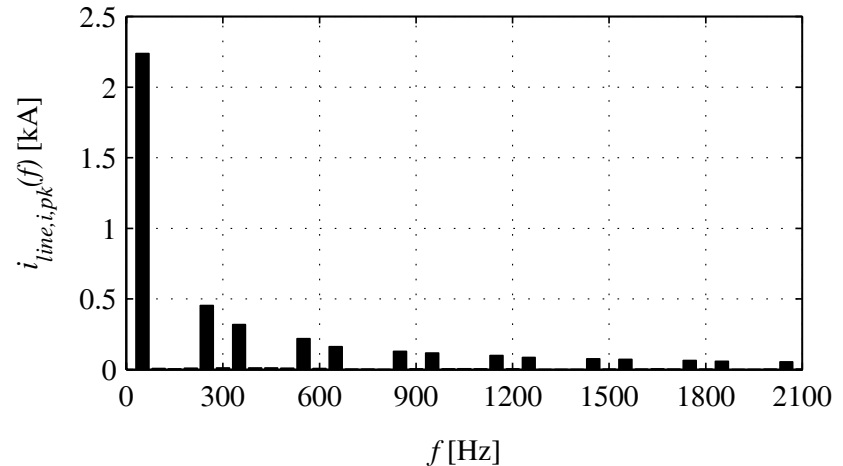
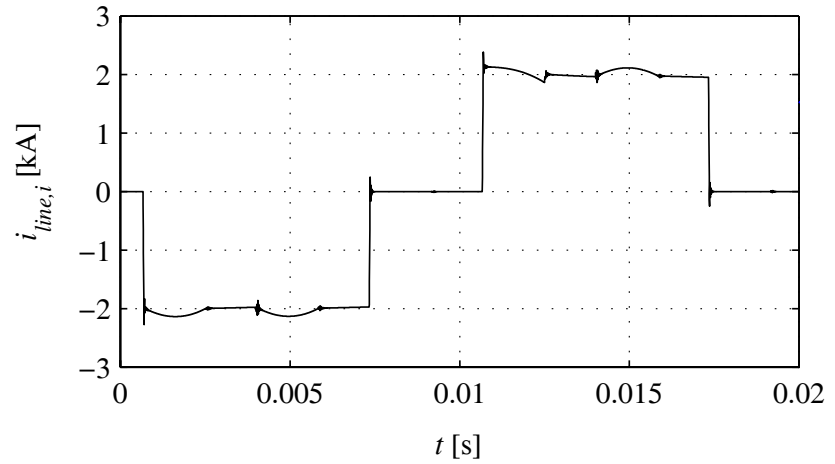


Figure 1.13: R-phase line current (top) and its spectrum (bottom) for the inverter of an HVDC transmission system.

Commutation Overlap

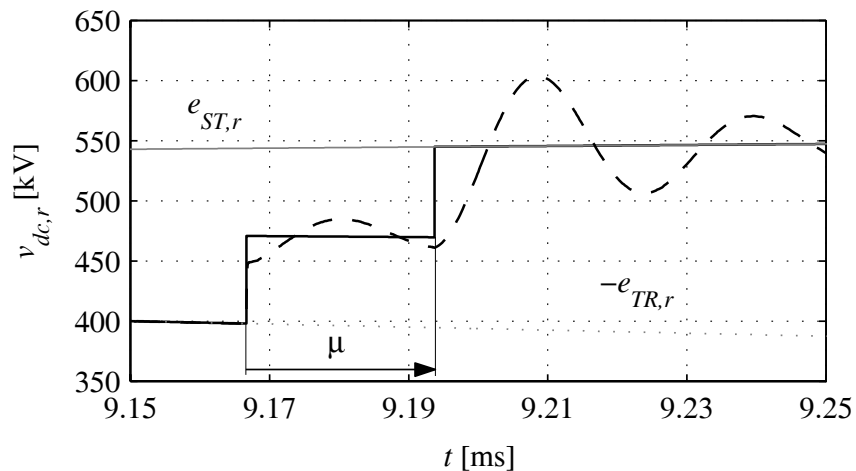
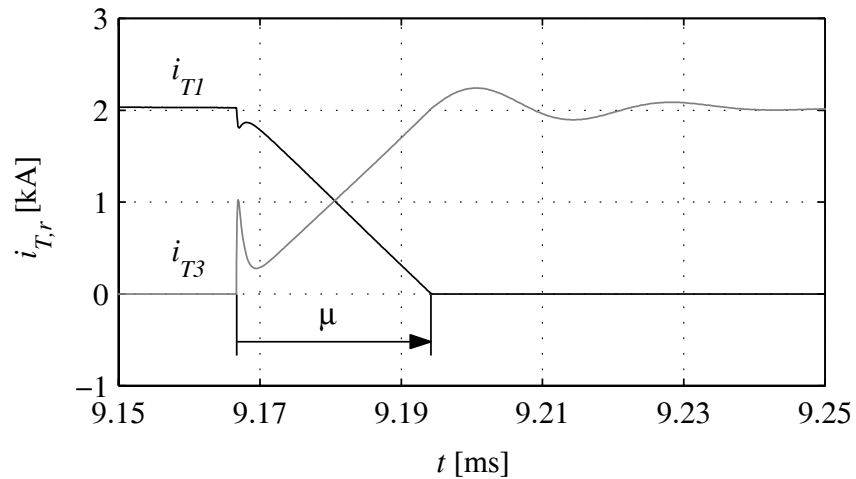


Figure 1.14: Commutation current (top) and voltage (bottom) for the rectifier.

The line inductance determines the commutation time, and therefore results in a loss of average voltage

$$V_{dcr} = V_{dc0} \cdot \cos(\alpha) - \Delta V_{dc} = V_{dc0} \cdot \cos(\alpha) - \frac{3}{\pi} \omega L_{line} I_{dc} =$$

$$= V_{dc0} \cdot \cos(\alpha) - \frac{3}{\pi} X_{line} I_{dc} = V_{dc0} \cdot \cos(\alpha) - R_{dcr} I_{dc}$$



Practical HVDC installations

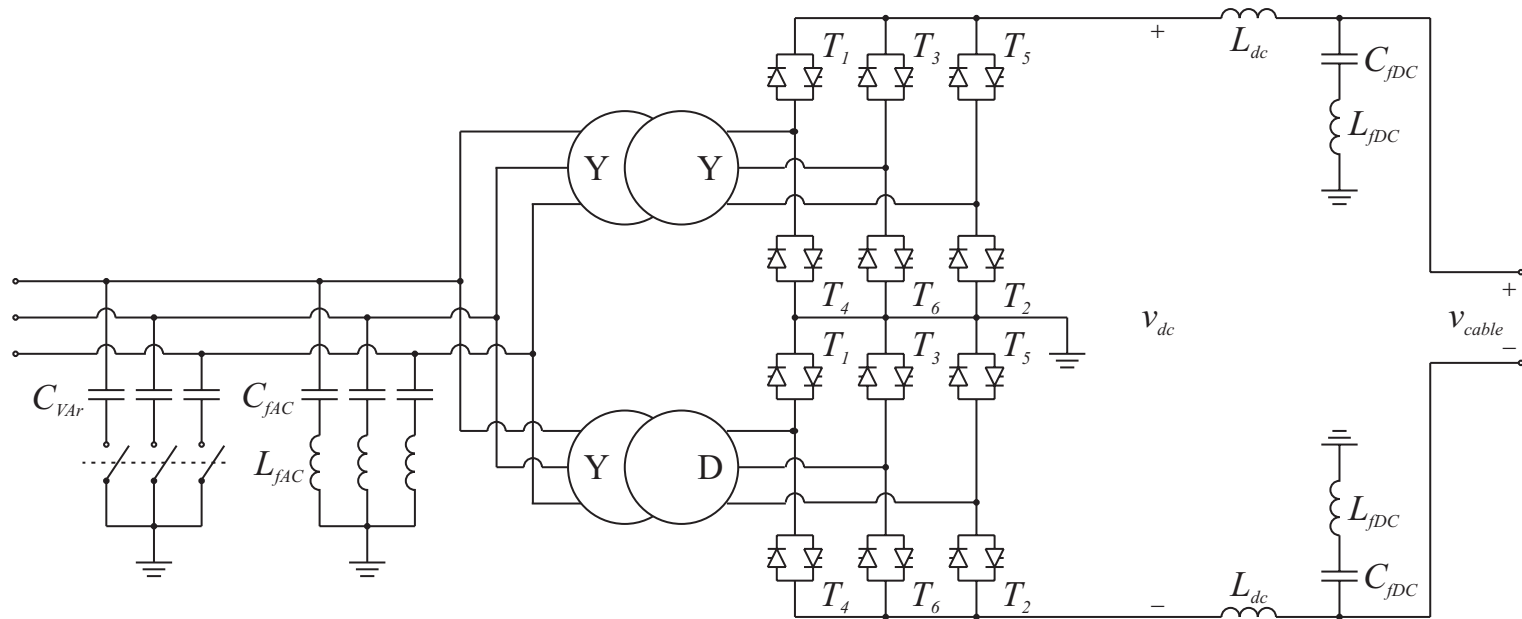


Figure 1.15: Realistic schematic of an HVDC power station.

The Buck Converter (Step-Down Converter)

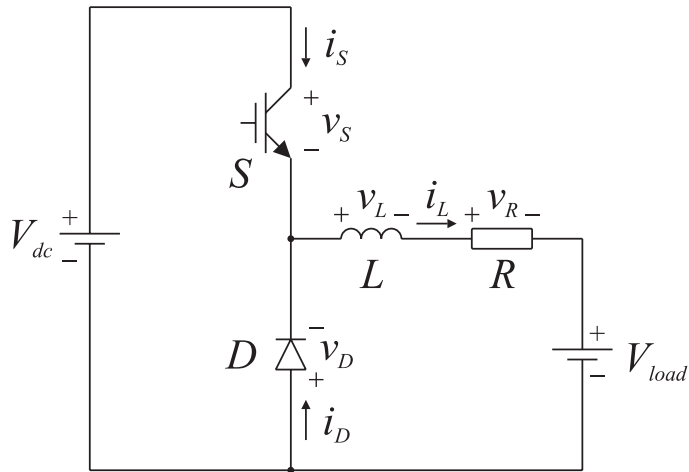


Figure 1.16: Buck converter.

S "on"

$$V_{dc} - V_{load} = v_L = L \frac{di_L}{dt} \Rightarrow \Delta i_L = \frac{V_{dc} - V_{load}}{L} \cdot DT_{sw}$$

S "off"

$$-V_{load} = v_L = L \frac{di_L}{dt} \Rightarrow \Delta i_L = -\frac{V_{load}}{L} \cdot (1-D)T_{sw}$$

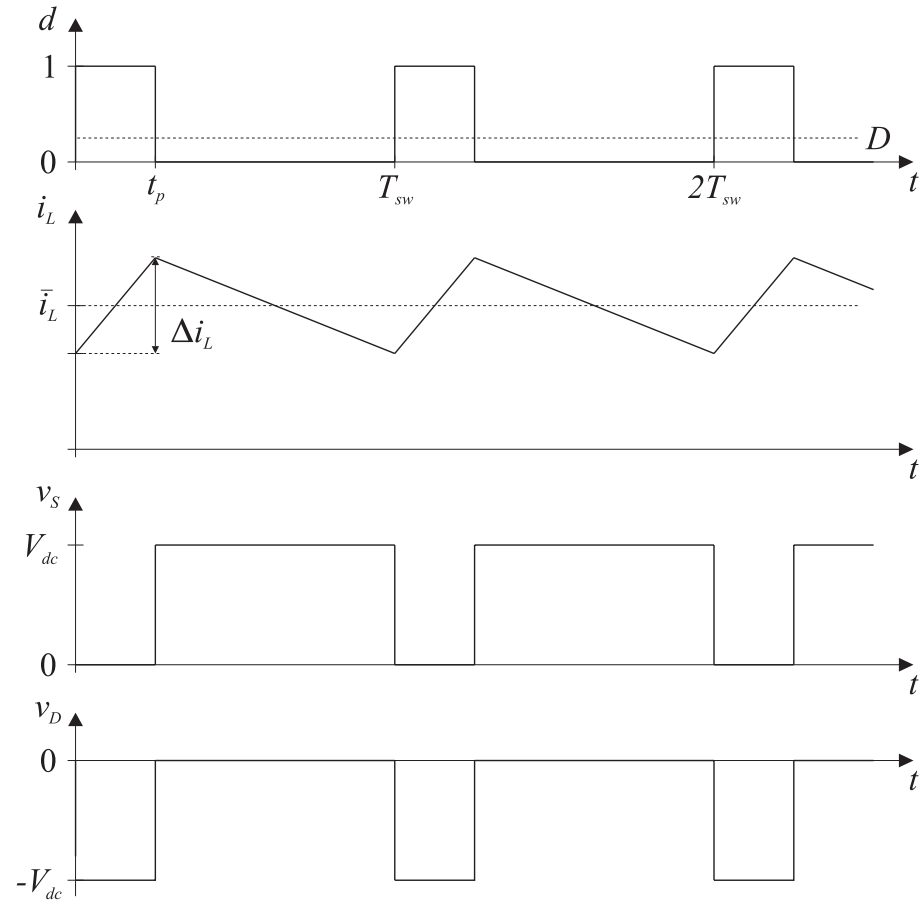


Figure 1.17: Ideal waveforms of the Buck converter.

The Boost Converter (Step-Up Converter)

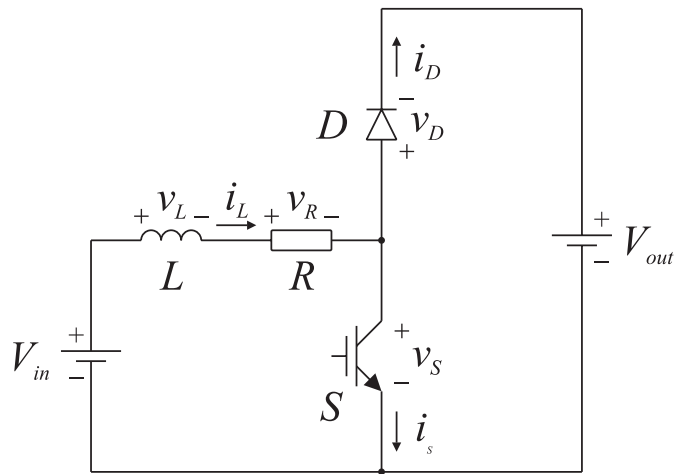


Figure 1.18: Boost converter.

S "on"

$$L \frac{di_L}{dt} = v_L = V_{in} - v_S \approx V_{in} \Rightarrow \Delta i_L = \frac{V_{in}}{L} \cdot DT_{sw}$$

S "off"

$$L \frac{di_L}{dt} = v_L = V_{in} - v_D - V_{out} \approx V_{in} - V_{out} \Rightarrow$$

$$\Delta i_L = \frac{V_{in} - V_{out}}{L} \cdot (1 - D)T_{sw}$$

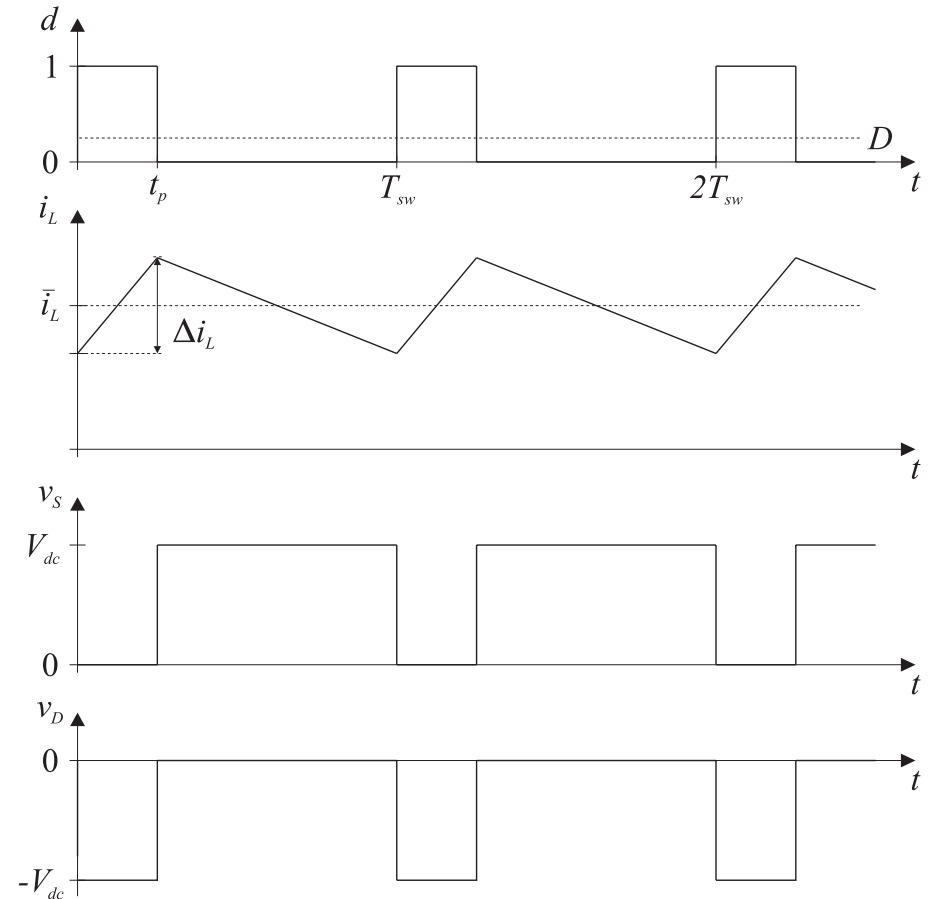


Figure 1.17: Ideal waveforms of the Boost converter. Replace V_{dc} and V_{load} of the Buck converter with V_{out} and V_{in}



The Buck-Boost Converter (Half-Bridge)

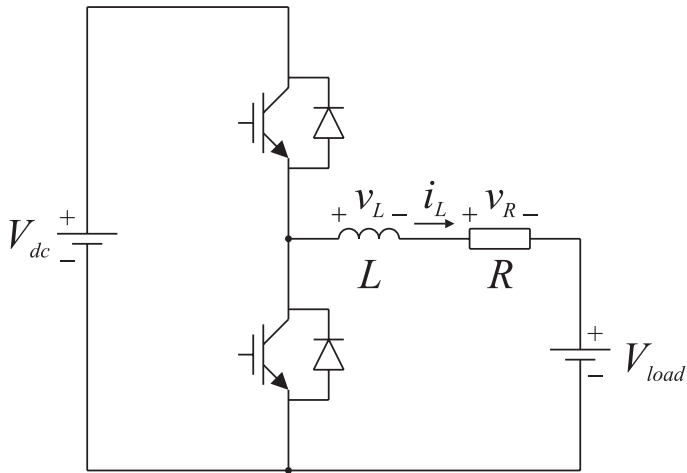


Figure 1.19: Buck-boost converter.

S "on"

$$V_{dc} - V_{load} = v_L = L \frac{di_L}{dt} \Rightarrow \Delta i_L = \frac{V_{dc} - V_{load}}{L} \cdot DT_{sw}$$

S "off"

$$-V_{load} = v_L = L \frac{di_L}{dt} \Rightarrow \Delta i_L = -\frac{V_{load}}{L} \cdot (1-D)T_{sw}$$

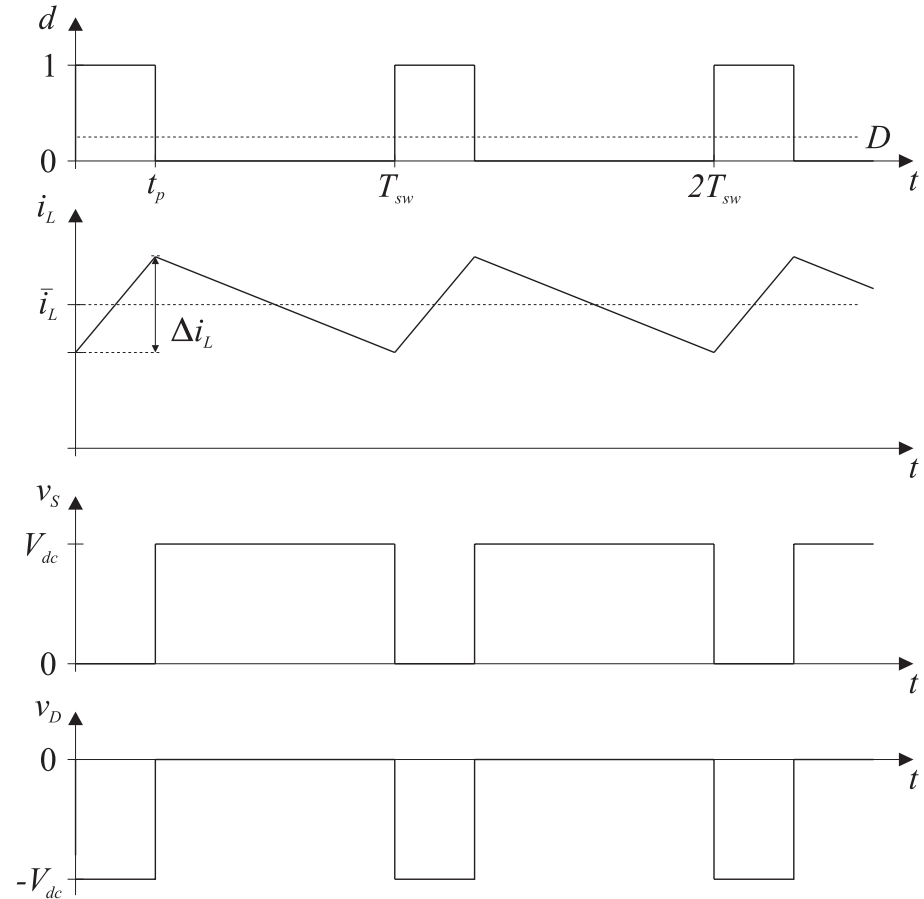
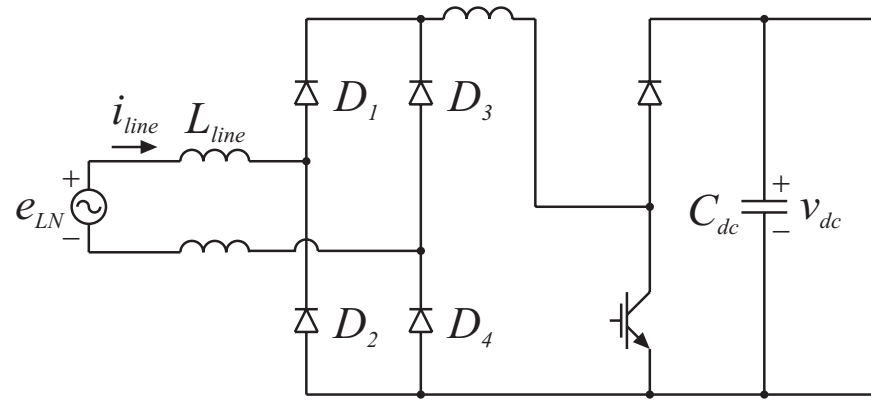


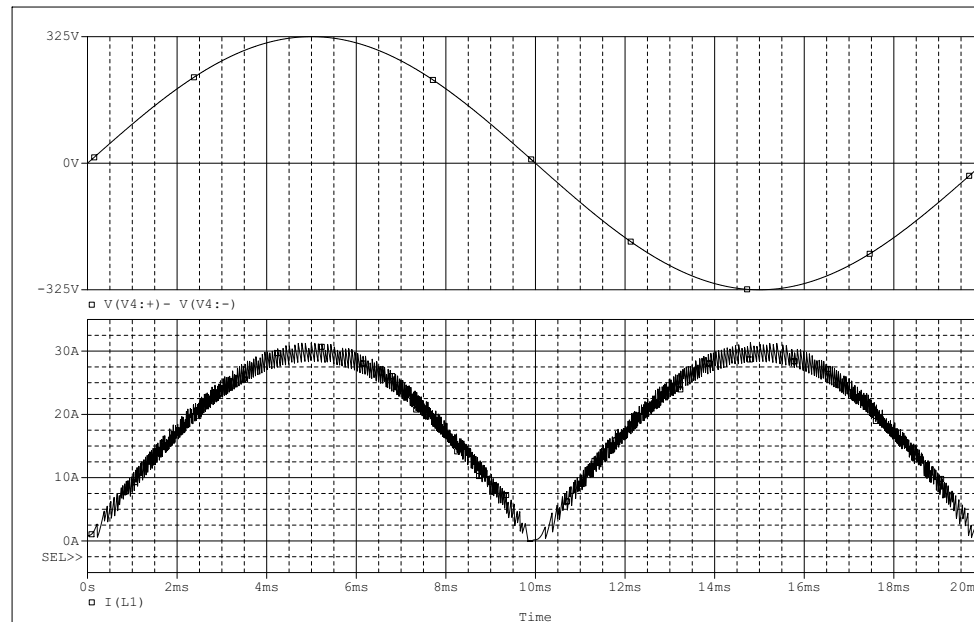
Figure 1.17: Ideal waveforms of the Buck-boost converter.



Diode rectifier with Power Factor Corrector



Single-phase diode rectifier with power factor corrector (PFC).



Line-to-neutral voltage (top) and rectified line current (bottom) for a diode rectifier equipped with PFC.

VSC Based HVDC

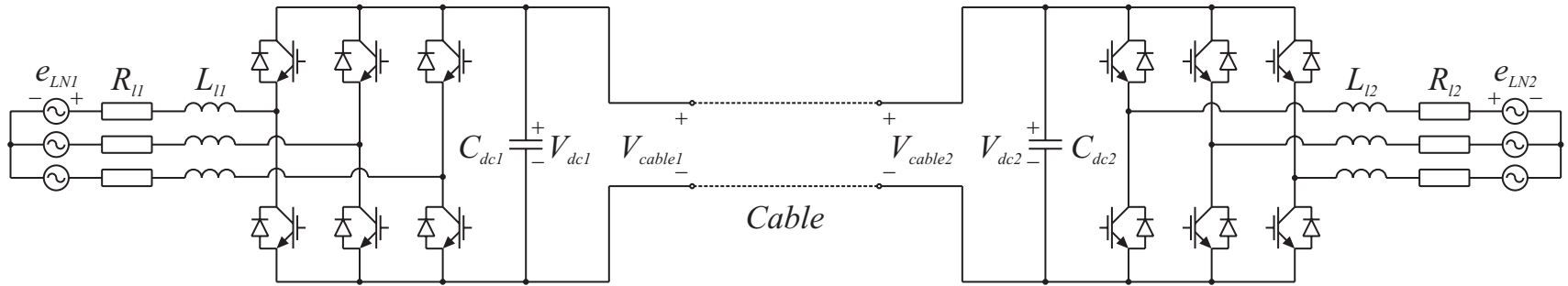


Figure 1.30 Basic VSC based HVDC power transmission interconnection.

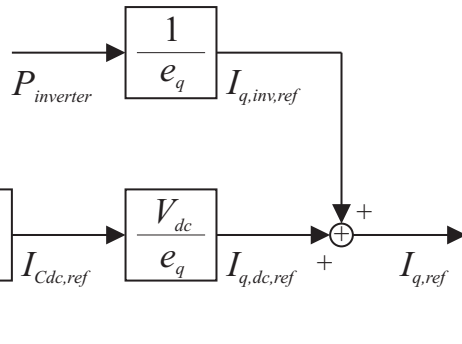


Figure 1.31 DC bus voltage controller for VSC based HVDC.

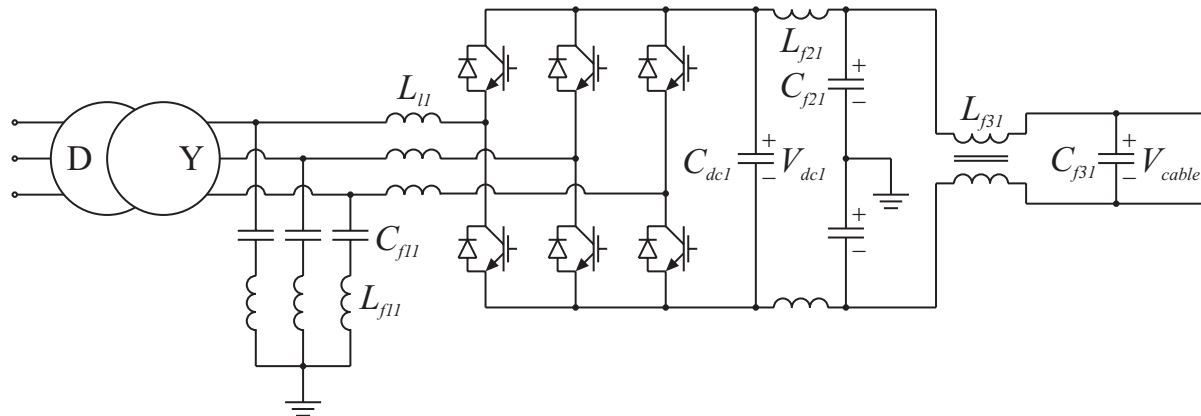


Figure 1.32 Realistic VSC based HVDC light converter station.