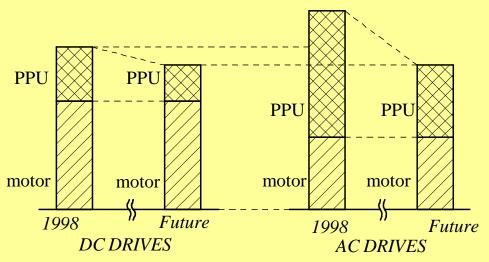
### DC Motor Drives

- Introduction
- Classification
- Structure
- Operating Principle
- Armature Reaction
- DC Machine Equivalent Circuit

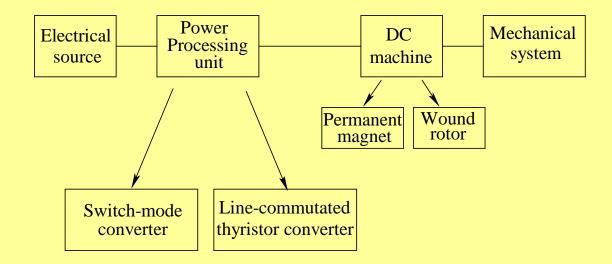
#### Introduction

☐ Cost

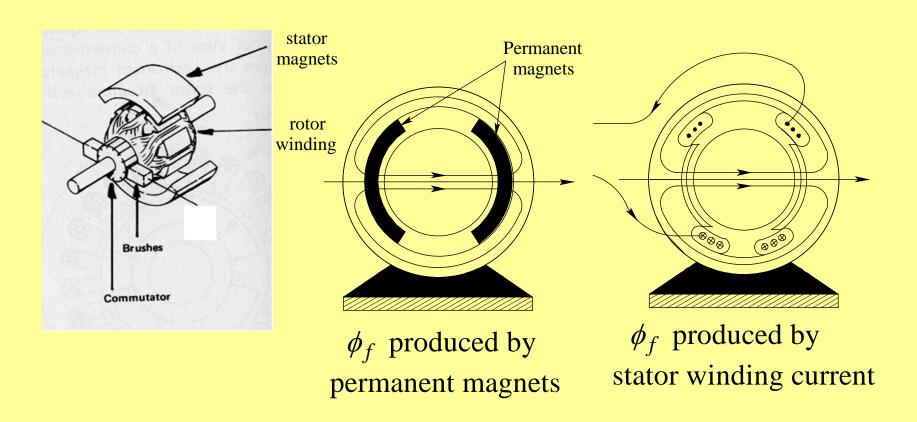


- ☐ Demise prematurely predicted, still used in speed control
- □ Merits
  - Ease of control
  - Cheaper Power Processing Unit
- ☐ Drawbacks
  - mechanical commutator and brushes require maintenance

### Classification of DC drives



### Structure of DC motors

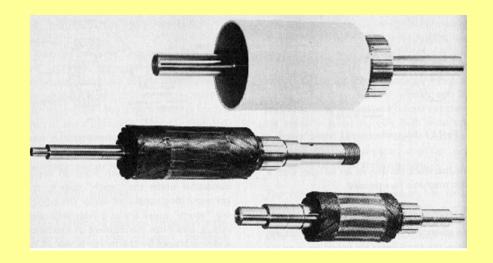


- ☐ Stator
  - ullet Establishes field flux,  $\phi_{\mathrm{f}}$

## Structure of DC motors

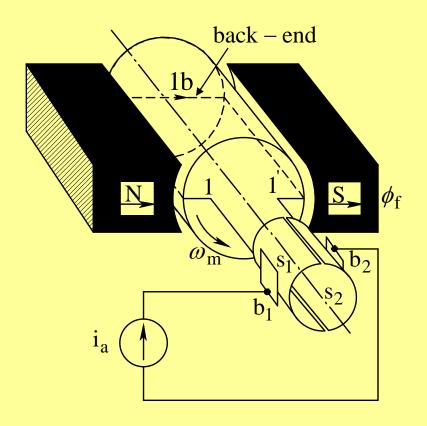
#### ☐ Rotor

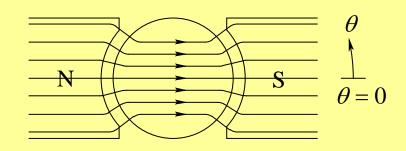
- ◆Armature winding
- ◆Commutator and brushes

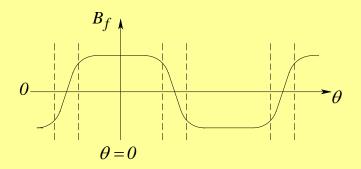


## Operating Principles of a DC Motor

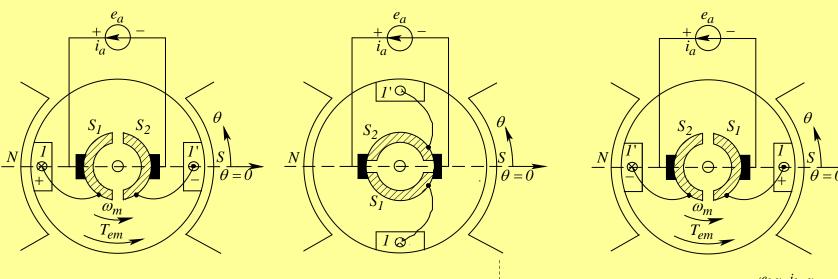
☐ Field flux density in the airgap





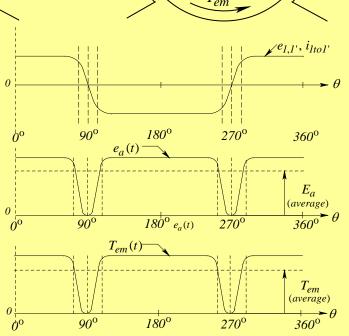


## Operating principles - Commutator Action

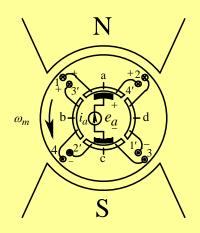


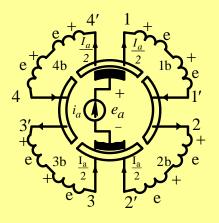
$$T_{em} = 2 B_f \ell i_a r$$

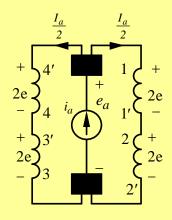
$$e_a = 2B_f \,\ell(r\,\omega_m)$$



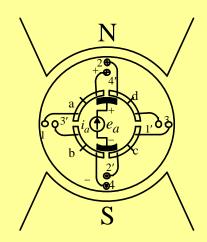
# Four Coil Example

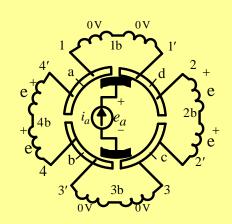


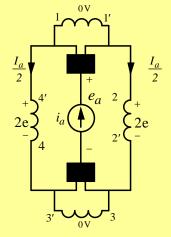






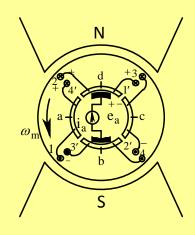


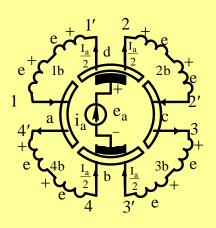


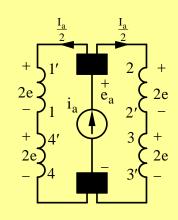


CCW rotation by 45°

## Four Coil Example (cont'd)

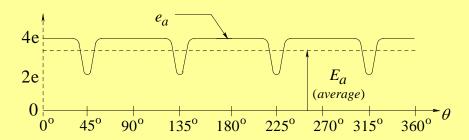


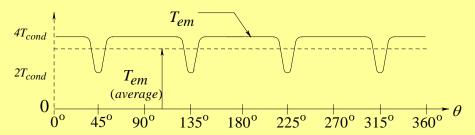




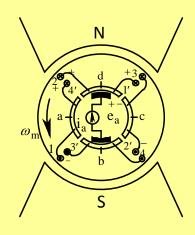
CCW rotation by 90°

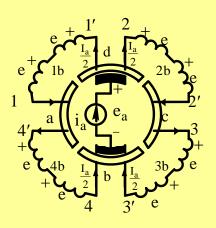
Torque and emf pulsations can be reduced by increasing the number of conductors

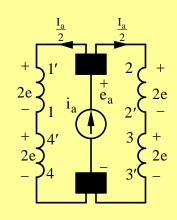




## Four Coil Example (cont'd)

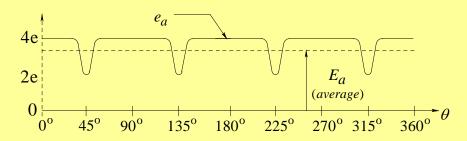


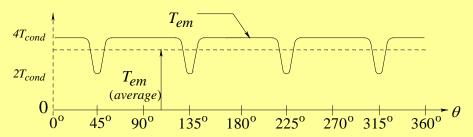




CCW rotation by 90°

Torque and emf pulsations can be reduced by increasing the number of conductors





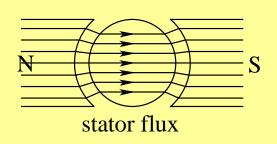
## **Summary of Operating Principles**

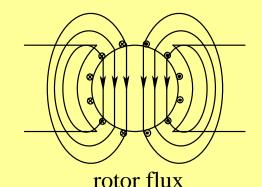
- $\bullet$   $i_a$  divides equally between two parallel circuits
- ◆ Torque produced on each conductor has the same direction
- lacktriangle Direction of  $i_a$  determines direction of torque
- ◆Induced voltage in each circuit is equal to the sum of voltages induced in each coil.
- ◆ Polarity of induced emf depends only on the direction of rotation.

Net Torque, 
$$T_{em} = n_a B_f \left(\frac{i_a}{2}\right) lr = \left(\frac{n_a}{2} lr B_f\right) i_a = k_T i_a$$
  
&  $e_a = \left(\frac{n_a}{2}\right) B_f l(\omega_m r) = \left(\frac{n_a}{2} lr B_f\right) \omega_m = k_E \omega_m$ 

In M.K.S. Units  $k_E = k_T$ 

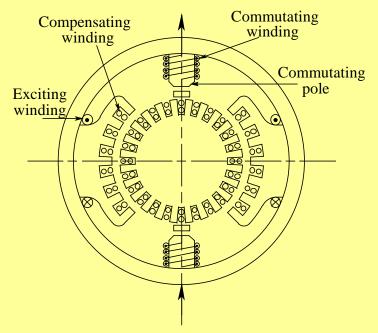
#### Armature reaction



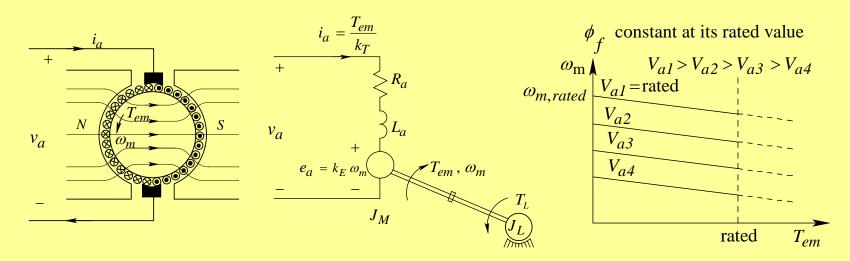




- ☐ Assuming magnetic structure does not saturate:
- ◆ Increased torque in some conductors is compensated by decreased torque in other conductors
- ◆ Same reasoning holds for induced emf
- ☐ Compensating winding to reduce the effect of armature reaction



## DC Machine Equivalent Circuit



#### **Basic equations**

$$e_a = k_E \omega_m$$

$$v_a = e_a + R_a i_a + L_a \frac{d i_a}{dt}$$

$$T_{em} = k_T i_a$$

$$\frac{d \omega_m}{dt} = \frac{1}{J_{eq}} (T_{em} - T_L)$$

#### **Steady State**

$$I_a = \frac{T_{em}(=T_L)}{k_T}$$

$$\omega_m = \frac{V_a - I_a R_a}{k_E}$$

# Summary

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